

# A Covariance Matrix Method for Accurate Bit Error Rates in a DWDM CRZ System

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# BER Calculation: Common Approaches

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- 1 **Full Monte Carlo simulations + Gaussian extrapolation** [Bergano]
  - + : few assumptions, simple
  - : computationally very expensive, pdfs are not Gaussian
- 2 **Optical white noise at receiver** [Marcuse, Winzer]
  - + : very fast, deterministic
  - : noise-free transmission, no signal-noise interaction
- 3 **CW transmission linearization + analytic pdfs** [Hui, Bosco, Mazurczyk]
  - + : very fast, deterministic, includes parametric gain
  - : no data modulation in signal-noise interaction during transmission

***None of these approaches is well-validated***

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# The Covariance Matrix Method

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R. Holzöhner, *et al.*, J. Lightwave Technol. **20**, pp. 389–400 (2002)

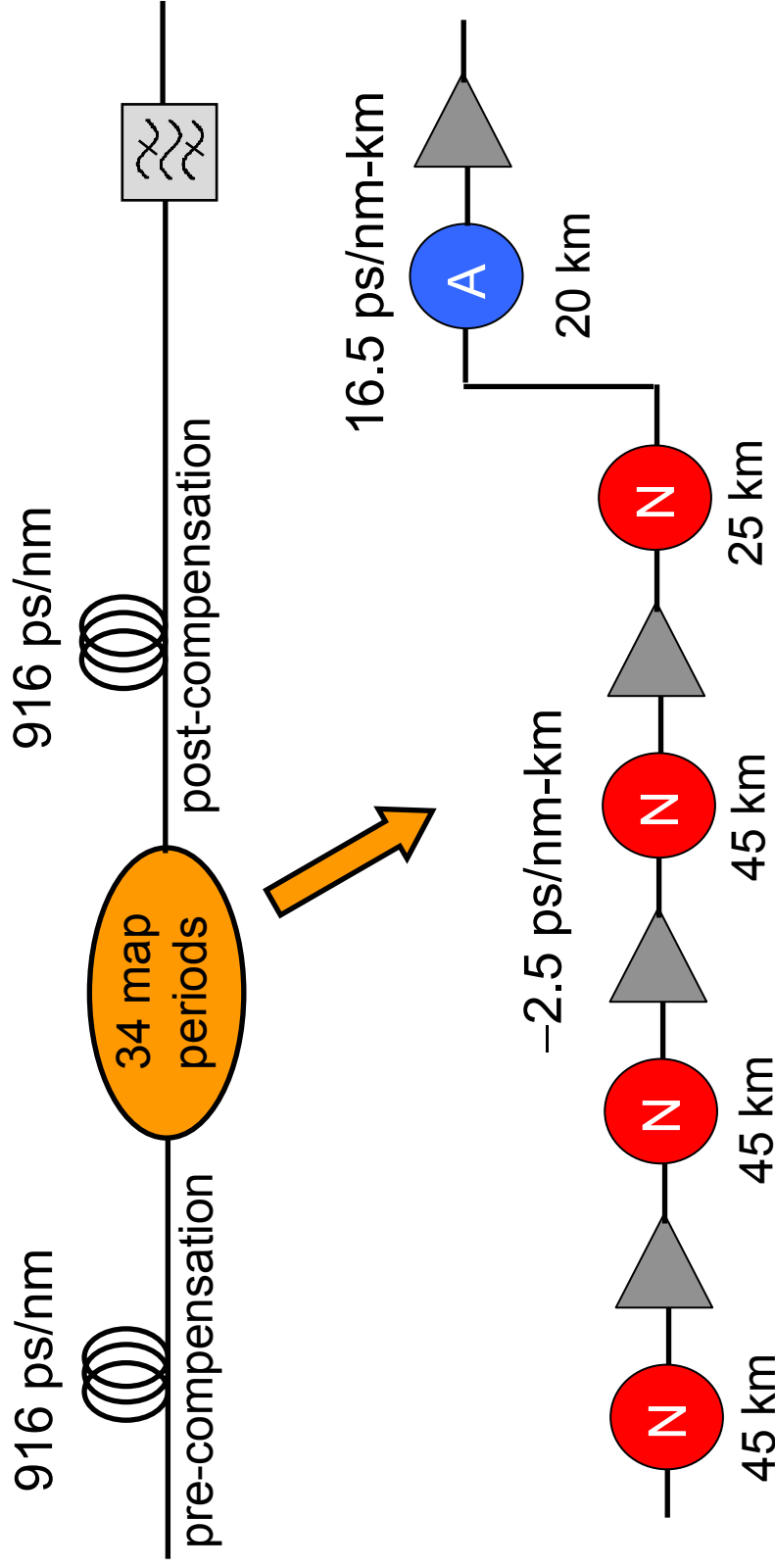
- **For modulated data with multiple bits and channels**
- **Deterministic fiber propagation model:**
  - Includes nonlinear interactions between signal and noise
  - Neglects nonlinear noise-noise interactions in the fiber
  - Propagates the optical noise covariance matrix
- **Receiver model includes:**
  - Realistic optical and electrical filters
  - Quadratic noise-noise interactions

***We compute the noise covariance matrix deterministically***

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# Test System: CRZ DWDM

Submarine 10 Gb/s CRZ system, 6100 km, 50 GHz channel spacing

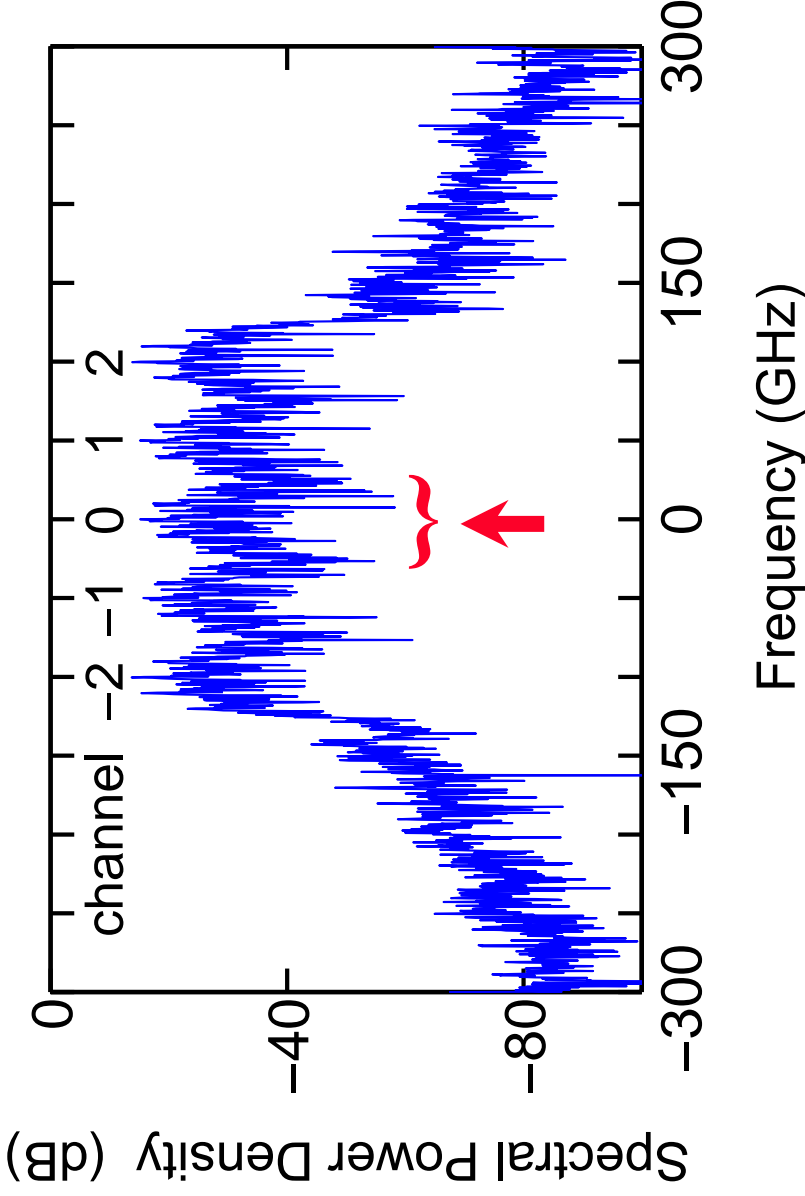


**Strong pulse overlap**

# DWDM System Modeling

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## Noise analysis for channel 0



32-bit PRBS  
in all channels  
(contains all  
5-bit patterns)

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***Simulating five channels is sufficient\****

\* Yu, et al., Photon. Technol. Lett. **12**, pp. 443–445 (2002)

# How to Compute the Covariance Matrix

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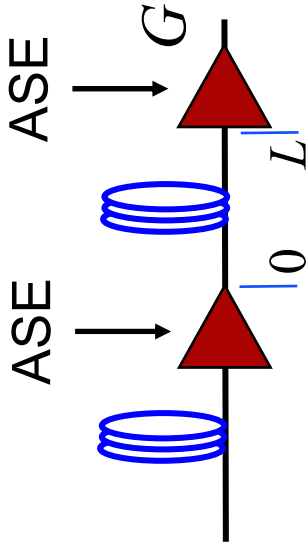
Linearize the nonlinear Schrödinger equation:

$$\frac{\partial \mathbf{a}}{\partial z} = \mathbf{R}(z) \mathbf{a} \Rightarrow \mathbf{a}(L) = \mathbf{\Psi} \mathbf{a}(0)$$

$$\mathbf{K}_{ij} = \langle \mathbf{a}_i \mathbf{a}_j \rangle, \quad \dim(\mathbf{K}) = 280 \times 280$$

$$\mathbf{K}(L) = G \mathbf{\Psi} \mathbf{K}(0) \mathbf{\Psi}^T + \eta \mathbf{I}$$

↑ ASE  
input



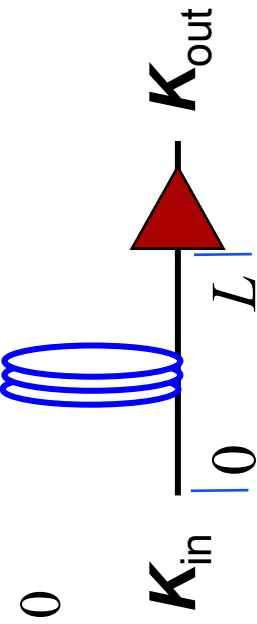
**Compute  $\Psi$  by perturbing each of the frequency modes separately**

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# Algorithm

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The following is done for each fiber span and each frequency  $k$ :

- 1 Perturb the noise-free signal in  $k$  at  $z = 0$
- 2 Filter out central channel at  $z = L$    $K_{\text{in}}$   $K_{\text{out}}$
- 3 Separate the pulses by compensating accumulated dispersion
- 4 Remove the phase jitter of each pulse, invert step 3

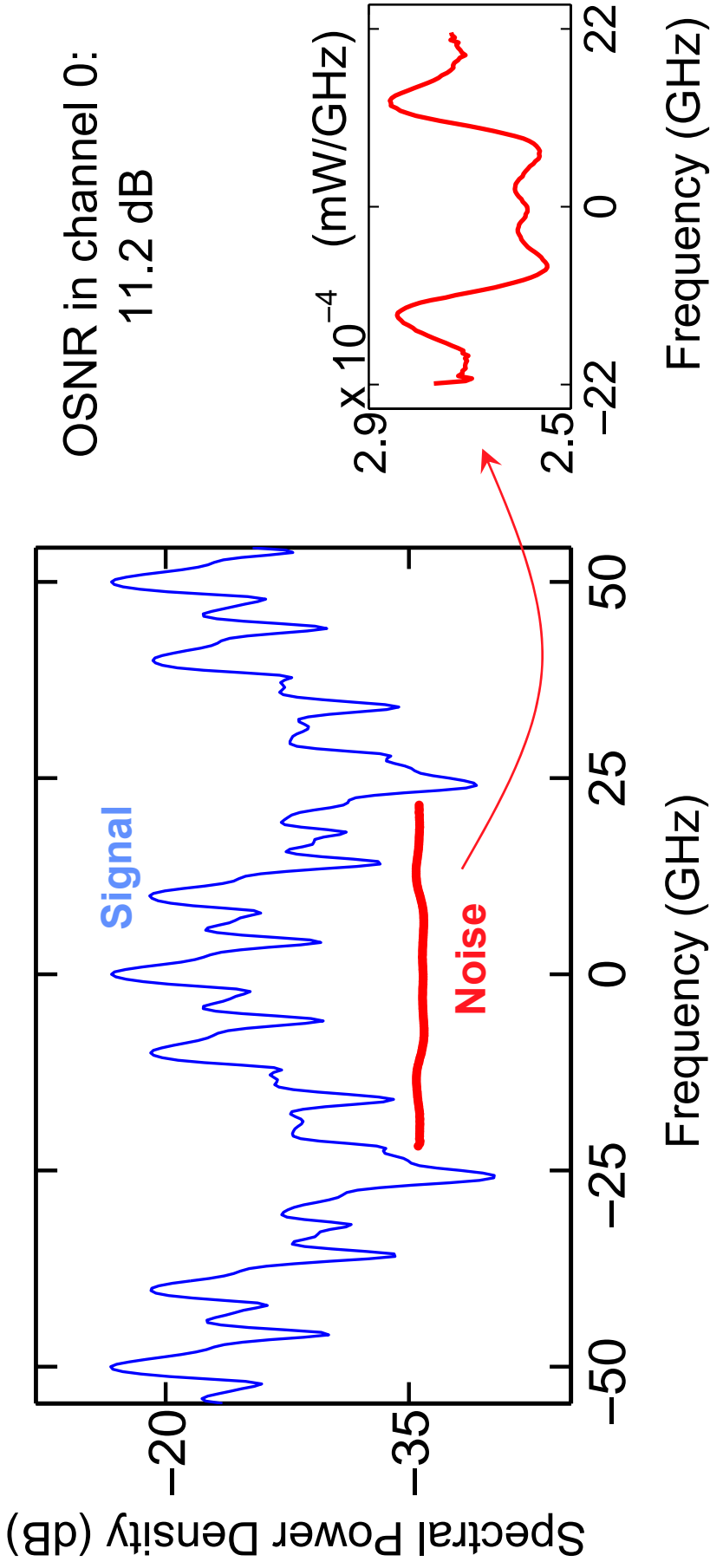
Evaluate  $\Psi$ , propagate the covariance matrix

***This approach neglects interchannel  
noise-noise correlations***

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# Results

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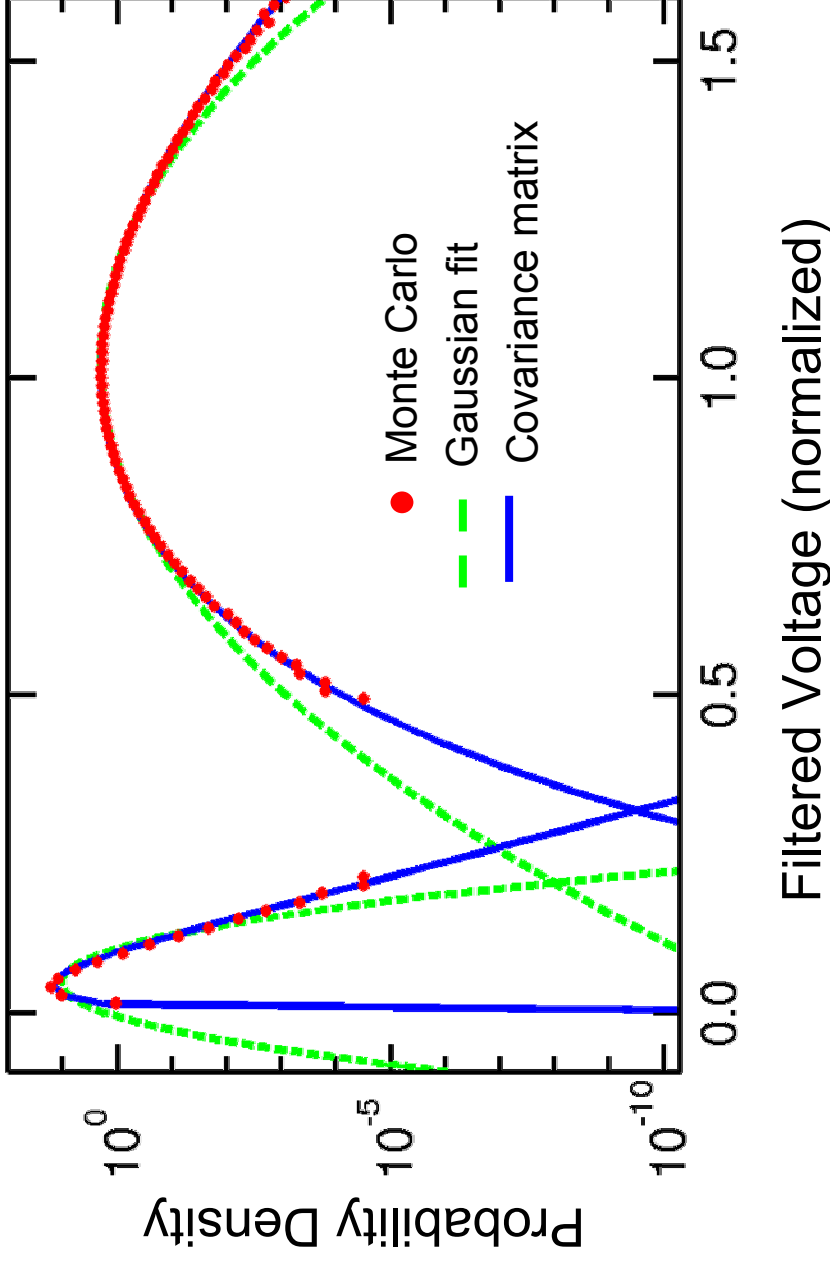
***Optical noise at the receiver is not white!***

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# Pdfs of the Electrical Voltage

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5 channels,  
32 bits

Optimum BER:  
 $3.1 \times 10^{-12}$

Optimum  
Gaussian BER:  
 $1.0 \times 10^{-11}$   
 $Q = 6.7$

***Excellent agreement between Covariance Matrix Method and Monte Carlo simulations\****

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\* Holzlohner, et al., CLEO 2003, talk CThJ, to appear

# Conclusions

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- 1 We validated the Covariance Matrix Method for a DWDM CRZ system
- 2 Number of relevant modes the same as in single-channel system
- 3 Good scaling behavior
- 4 Computational cost equals 280 noise-free simulation runs!

***Covariance Matrix Method is highly accurate  
and relatively fast***

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