Thin Cloud Removal Based on Signal Transmission Principles and Spectral Mixture Analysis

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Abstract—Cloud removal is an important goal for enhancing the utilization of optical remote sensing satellite images. Clouds dynamically affect the signal transmission due to their different shapes, heights, and distribution. In the case of thick opaque clouds, pixel replacement has been commonly adopted. For thin clouds, pixel correction techniques allow the effects of thin clouds to be removed while retaining the remaining information in the contaminated pixels. In this paper, we develop a new method based on signal transmission and spectral mixture analysis for pixel correction which makes use of a cloud removal model that considers not only the additive reflectance from the clouds but also the energy absorption when solar radiation passes through them. Data correction is achieved by subtracting the product of the cloud endmember signature and the cloud abundance and rescaling according to the cloud thickness. The proposed method has no requirement for meteorological data and does not rely on reference images. Our experimental results indicate that the proposed approach is able to perform effective removal of thin clouds in different scenarios.

Index Terms—Cloud removal, cloud thickness, data correction, signal transmission, spectral unmixing.

I. INTRODUCTION

REMOTE sensing satellite images generated using frequencies in the optical to microwave electromagnetic spectrum have been widely applied in Earth Observation. Optical remote sensing, in particular, is popular since it is relatively easier to interpret and analyze. Recently, new optical multispectral data have become available from Landsat 8 Operational Land Imager (OLI), which was launched in 2013 [1] and SPOT 7, which was launched in June 2014 (http://www.astrium-geo.com) These sensors provide continued monitoring of land surface, ocean, and atmosphere with medium and high spatial resolution. However, one of the primary limitations of optical sensors is their sensitivity to atmospheric conditions. Cloud cover is a key problem which degrades the utilization of optical data and increases the difficulty of image analysis [2], [3]. Clouds dynamically affect the electromagnetic signal transmission due to their different shapes, heights, and distribution. Thick opaque clouds may block all the reflectance from the Earth’s surface, while thin transparent clouds attenuate the incident energy to the ground and contaminate the upwelling signal received by the sensor [4]. Data replacement for the blocked areas and data correction for the distorted pixels are a valuable pre-processing step to restore the quality of collected images for subsequent applications. [5] proposed a method which uses similar pixels in neighboring areas of the target image to fill the blocked pixels, and multitemporal data are required as a reference to identify similar pixels. In addition, Li et al. [6] introduced a multitemporal dictionary learning approach to achieve thick cloud replacement. In this paper, we mainly address the data correction issue, i.e., removing the effect caused by thin clouds.

To derive cloud free images, identifying cloud affected pixels using cloud detection techniques is a primary task. An automated cloud-cover assessment (ACCA) algorithm was designed to estimate the fraction of cloud cover in images captured by the ETM+ on Landsat 7. ACCA makes use of the spectral properties of landscape features and cloud signatures in the thermal band (Band 6 of ETM+) to mask cloudy pixels [7], [8]. In [9], the author developed the function of mask (Fmask) algorithm for detecting cloud and cloud shadow in Landsat imagery over land and water, separately. Fmask improved the cloud detection performance when compared with ACCA and addressed the snow interference issue. Several methods, using multispectral analysis, have been proposed to identify cloud cover based on an assumption that cloud is normally brighter and colder than the underlying land surface [10], [11]; however these methods will fail when the cloud is relatively thin and warm [9]. Gao et al. [12] proposed a method to detect cirrus cloud using the 1.38 µm band from MODIS. This short wave infrared band has very strong water vapor absorption, such that only high level clouds in the atmosphere are visible in this narrow band and the ground appears totally black [13]. A multi-temporal cloud detection (MTCD) method was presented in [14] by taking advantage of the high revisit frequency of Landsat sensors and was shown to be able to identify any significant increases in reflectance on a per pixel basis between cloudy images and cloud-free images acquired on different dates. However, the result produced by MTCD is strongly dependent on the quality of the reference images. More sophisticated detection methods have been proposed in recent years based on image fusion [15], [16], neural networks [17] and a Bayesian approach [18].

Several methods have been developed to retrieve the reflectance from the objects beneath the cloud. The dark object subtraction algorithm [19], [20] is simple and effective for approximate bulk correction of atmospheric effects, with no
 requirement for meteorological data [4]. The haze optimized transformation (HOT) was proposed in [21] based on the observation that spectral responses of various types of land surfaces in the red band have high correlation to the blue band under clear atmospheric conditions [22]. This linear relationship will be contaminated when clouds are present. Therefore, cloud removal was implemented by moving the cloudy pixels’ data to the clear line which represents the linear relationship of the two bands in spectral space. A principal component based haze masking approach was developed in [23] which combines spatial and spectral features of cloud in the transformed space. While these image-based methods are easy to implement, the haze masking approach was developed in [23] which combines spatial and spectral features of cloud in the transformed space.

Another weakness of these models is the lack of consideration of cloud absorption. In this paper, we develop an improved cloud model to include the cloud absorptance in the signal transmission path.

Alternatively several cloud screening methods have been developed based on spectral unmixing techniques [30]–[32]. Due to limited spatial resolution, most pixels in a remote sensing image are mixed pixels and they contain more than one ground cover type (endmember classes). The spectrum of a pixel recorded by satellite scanners is often a mixture of the reflectance from more than one distinct material. Spectral unmixing techniques have been developed to find the fraction (abundance) of each endmember class [33]–[35]. The paper [30] treated cloud as one of the endmember classes and selected a pure cloud spectrum as the endmember to represent the cloud signature. The cloud-abundance product is obtained after mixture model inversion. A linear mixture of cloud and background modeled for MODIS radiance was proposed in [32], where cloud fractions were estimated by a multiple-kernel learning-based unmixing algorithm. These methods yield subpixel cloud fraction results. Cloud effect removal, however, was not addressed. In this paper, we combine spectral unmixing analysis with the physical model to achieve data correction.

More specifically, we develop a new cloud removal method based on signal transmission and spectral mixture analysis (ST-SMA) which considers not only the additive reflectance from clouds but also the energy absorption when solar radiation passes through them. Spectral unmixing is applied to estimate cloud thickness, which is equivalent to the cloud abundance within a pixel. Data correction is finally achieved by subtracting the product of the cloud endmember signature and the cloud abundance and rescaling according to the cloud thickness.

The rest of this paper is organized as follows. Section II briefly reviews related work on physical cloud distortion modeling and linear spectral mixture analysis used in cloud mapping. Section III describes the proposed method ST-SMA for modeling cloud effects and correcting cloud contamination. Section IV presents a series of experiments to validate the ST-SMA approach. Finally, discussions and conclusions are given in Section V.

II. RELATED WORK

A. Cloud Distortion Model

A physical model of cloud distortion was first developed in [24]. The authors assumed that the received signal at the sensor is given by

$$s(x, y) = a I r(x, y) t(x, y) + I [1 - t(x, y)]$$  \hspace{1cm} (1)

where $I$ is the solar irradiance, $r(x, y)$ is the reflectance from ground, and $t(x, y)$ is the cloud transmittance. $a$ is the sunlight attenuation coefficient. The values of $a$, $r(x, y)$ and $t(x, y)$ range from 0 to 1. The first part of (1) indicates the degraded reflectance from the ground, and the second part denotes the reflected signal from cloud with an assumption of 0% cloud absorption. After subtracting $s(x, y)$ from $I$ and taking the logarithm, we obtain

$$\log [I - s(x, y)] = \log [I - a I r(x, y)] + \log [t(x, y)]$$ \hspace{1cm} (2)

where $\log[I - a I r(x, y)]$ and $\log[t(x, y)]$ are associated with the original signal and cloud noise, respectively. Thus, cloud removal can be conducted by using a homomorphic Weiner filter in the frequency domain by assuming that clouds contain only low spatial frequencies.

This distortion model considers the spectral characteristics of clouds. It treats the sum of reflectance and transmittance from cloud as one, with an assumption of zero cloud absorption. Therefore, the loss of radiation energy when passing through clouds is not considered. In fact, clouds have variable structure and thickness. Therefore, it is important to quantify the loss of energy when estimating cloud effects. Another weakness of this method is that there is a need to estimate the noise statistics of the cloud, which is nontrivial.

B. Cloud Assessment Using Spectral Unmixing Techniques

The limited spatial resolution of sensors and the complexity of Earth surface materials usually lead to mixed pixels in most areas of a remote sensing image. Spectral unmixing is a technique that is used to address the mixture problem by decomposing a mixed spectrum into a fractional set of spectra of pure materials (known as endmembers) [33], [35]. Cloud assessment using spectral unmixing techniques has taken the approach of treating cloud as one of the endmembers. Suppose there are $M$ endmembers in the mixed pixel. When a linear mixture model is applied, the reflected solar electromagnetic radiation $x$ can be expressed as

$$x = \sum_{m=1}^{M} a_m s_m + e = Sa + e$$ \hspace{1cm} (3)
where $x$ is an $L \times 1$ column vector, representing the reflectance of the observed pixel, $L$ is the number of spectral bands in the image, $S = (s_1, \ldots, s_M)$ denotes an $L \times M$ endmember signature matrix whose $m$th column vector represents the $m$th endmember signature. $a = (a_1, \ldots, a_M)^T$ is an $M \times 1$ abundance vector representing the fraction of each endmember. $e$ is an $L \times 1$ noise vector which can be considered as model error.

A cloud-screening algorithm that used spectral unmixing techniques to produce a cloud abundance map instead of binary indicators for cloud or non-cloud was developed in [30]. In their model, cloud is assumed to be one of the endmember signatures. Cloudy pixels in the given band $l$ are considered separately. The attenuation of the sunlight during the propagation of cloud is ignored. It is also worth noting that this method is mainly for cloud assessment. While the cloud fractions were mapped, cloud effect removal could bring additional issues, which were not presented in [30].

In this paper, we address the aforementioned issues by presenting a new method, ST-SMA, which can estimate the absorption and transmission for various thicknesses of cloud, and achieve cloud removal with the aid of spectral unmixing techniques.

### III. PROPOSED METHOD

#### A. Physical Cloud Effect Modeling

The proposed cloud removal method ST-SMA starts with the application of an electromagnetic energy balance equation. During propagation of solar radiation, scattering and absorption occurs [37]. Scattering can occur in two ways, reflection and transmission. The sum of reflected, transmitted, and absorbed radiation equals the incident radiation according to the law of conservation of energy [38]. This fact can be expressed as

$$ I = R + A + T $$

where $I$ is the incident radiation, $R$ is the reflected radiation, $A$ is the absorbed radiation, and $T$ is the transmitted radiation. If we use reflectance $\rho_r$, absorptance $\rho_a$, and transmittance $\rho_t$ to describe (7), then $R = \rho_r I$, $A = \rho_a I$ and $T = \rho_t I$. (7) can be rewritten as

$$ \rho_r + \rho_a + \rho_t = 1. $$

Based on this principle, we propose a means to estimate cloud transmittance as a function of cloud thickness. We first consider the relationship between an opaque cloud’s spectral reflectance and its absorptance, as shown in Fig. 1. We regard this case as zero transmittance, i.e., no sunlight is transmitted through the opaque cloud and all the remaining energy is absorbed by cloud after reflection. Therefore, the absorptance of opaque clouds is given by

$$ \rho_a = 1 - \rho_r, $$

where $\rho_r$ and $\rho_a$ are the reflectance and absorptance of opaque cloudy pixels in the given band $l$, respectively. In this case, transmittance $\rho_t = 0$.

To find the cloud absorptance, the cloud spectral reflectance characteristics need to be defined. While there is a general understanding of high reflectance over the wide range of spectral wavelengths from visible to mid infrared, the cloud spectrum is more reliably extracted from the image data of the current scene to accommodate the local conditions. We assume that pure cloud pixels exist in the cloudy imagery, and this pure cloud is opaque enough to block all sunlight from reaching the Earth’s surface. In general, thick clouds are much brighter than the land surface in visible bands. It should be mentioned that snow also emerges with very high reflectance in visible bands. Therefore, the presence of snow may cause errors in the cloud spectrum extraction process. However, snow reflectance drops significantly in shortwave-infrared bands while cloud still reflects a large proportion of solar radiation in this spectral region [39]. According to these characteristics of clouds, we propose to extract the cloud signature by searching for

$$ \arg \max_n \sum_{l=1}^L x_n(l), \; n = 1, 2, \ldots, N $$

where $x_n(l)$ is the reflectance of the $n$th pixel in the $l$th spectral band. $L$ and $N$ are the number of bands and total number of pixels in the image, respectively. If the sum of reflectances at each band $x_n$ is maximal, then the pixel is regarded as pure cloud. To reduce the effect of noise, the top few pixels may be identified, and their averaged spectrum is adopted as the cloud signature.
spectrum. Let $s_c$ be the vector representing the cloud spectrum, which will be used in the following derivation.

Obviously thinner clouds reflect less and absorb less, and hence transmittance is no longer zero. Let $\Gamma$ represent cloud thickness. When $\Gamma = 1$, we have the case of opaque cloud. If $\Gamma = 0$, we have the cloud free case, which means 100% transmittance without reflection and absorption. $\Gamma$ lies between 0 and 1 in other cases. Fig. 2 depicts the relationship between reflection, absorption, and transmission when solar radiation propagates through transparent thin clouds. We assume the reduced reflectance and absorptance, which become $\hat{r} = r - \Gamma r$ and $\hat{a} = a - \Gamma a$ at a given band $l$, respectively, are both proportional to the thickness factor $\Gamma$. For example, if $\Gamma = 0.2$, the reflectance and the absorptance will be reduced by 20%, then the transmittance through the cloud is $1 - 0.2r - 0.2a = 0.8$ (note that $r + a = 1$ for opaque clouds). Based on (8) and (9) the thin cloud transmittance $\hat{t}$ can be defined by

$$\hat{t}_l = 1 - \Gamma r - \Gamma a = 1 - \Gamma.$$  

(11)

This represents the transmitted radiation that reaches the Earth’s surface. Fig. 3 illustrates the signal interactions between the sun, the cloud, and the Earth’s surface. If the spectral reflectance of a given pixel on the ground is $r$ (an $L \times 1$ vector), the signal collected at the sensor becomes

$$x = (1 - \Gamma)r + \Gamma s_c + e$$  

(12)

where $x$ is an $L \times 1$ column vector representing the observed pixel value and $\Gamma s_c$ denotes the contributed cloud signal from the cloud. (12) represents the physical model of the effect of cloud on the recorded signals. In (12), there are $L + 1$ unknowns in the $L$ simultaneous equations, apart from the error term. They are the cloud thickness $\Gamma$ and the reflectance at $L$ bands, $r$, of the given pixel. Therefore, cloud removal cannot be resolved using this model alone. In the next section, we introduce spectral mixture analysis to solve this problem.

B. Geometric Modeling of Mixed Pixels on the Ground

Considering the pixel on the ground which receives the attenuated solar radiation due to the cloud effect, the reflected signal is determined by the spectral characteristics of the materials present in the corresponding pixel. Often there is more than one material due to the limited spatial resolution of the sensors. We adopt linear spectral unmixing techniques to decompose the reflected signal from the ground, $r$, as a weighted sum of $M$ endmembers as follows:

$$r = \sum_{m=1}^{M} a_m s_m + e$$  

(13)

where $a_m$ is the proportion of the $m$th endmember. To make the analysis meaningful, fully constrained least squares unmixing can be applied [36]. $a_m$ can be interpreted as the fraction of a pixels area that the $m$th endmember occupies. Therefore, we can call this model a geometric description. (13) is different from (3). In (3), cloud is one of the endmember classes, which is not the case in (13). In our cloud model, we separate cloud from the other materials present in the pixel on the Earth’s surface.

Endmember extraction is an important issue to address. A large number of unsupervised endmember extraction algorithms (EEAs) have been developed, e.g., Pixel Purity Index [40], [41], N-FINDR [42], vertex component analysis (VCA) [43], and minimum volume constrained non-negative matrix factorization [44], among many others [35]. When these methods are applied, a cloud endmember may be identified as well. However, in our method the cloud endmember needs to be treated separately as discussed in the next section. Supervised endmember extraction is more effective, when training data for pure classes are available to use. The endmember spectrum can be derived by averaging the training data. When the number of endmembers is fewer than the number of measurements, i.e., the number of spectral bands, an overdetermined problem is formed which can reduce the effect of noise and provide better estimates of the fraction of each endmember class using the least squares solution.

This geometric model will be combined with the physical model in the next section. A cloud removal method will then be generated.

C. Cloud Removal Model

The proposed cloud removal model ST-SMA is achieved by combining the physical analysis of the cloud effect and the
geometric description of the mixed reflectance from the ground as detailed below. If we substitute (13) into (12), we have

\[ x = (1 - \Gamma) \sum_{m=1}^{M} a_m s_m + \Gamma s_c + e \]  \hspace{1cm} (14)

s.t. \[ \sum_{m=1}^{M} a_m = 1, \quad a_m \geq 0, \quad 0 \leq \Gamma \leq 1. \]  \hspace{1cm} (15)

If we let \( a_{M+1} = \Gamma / (1 - \Gamma) \) and \( s_{M+1} = s_c \), (14) becomes

\[ x = (1 - \Gamma) \sum_{m=1}^{M+1} a_m s_m + e. \]  \hspace{1cm} (16)

Then if we let \( b_m = (1 - \Gamma)a_m \), (16) becomes

\[ x = \sum_{m=1}^{M+1} b_m s_m + e \]  \hspace{1cm} (17)

s.t. \[ \sum_{m=1}^{M+1} b_m = 1 - \Gamma, \quad 0 \leq b_m \leq \Gamma, \quad 0 \leq \Gamma \leq 1. \]  \hspace{1cm} (18)

We can see that (17) has a form similar to the standard form of LSMM, but with different constraints. Also, in the proposed model we can interpret cloud as one of the endmember classes. Then the new endmember signature matrix can be considered as \([s_1, s_2, \ldots, s_M, s_c]\). \( \Gamma \) can be regarded as cloud fractional abundance. In the aforementioned set of simultaneous equations (L equations), there are \( M + 1 \) unknowns, i.e., \( M \) fractions for \( M \) endmembers, plus the cloud thickness factor \( \Gamma \). As long as \( L > M + 1 \), all the unknowns can be estimated with the new constraints. After \( \Gamma \) is estimated, the cloud effect can be removed as follows for \( 0 \leq \Gamma < 1 \):

\[ x^* = \frac{1}{1 - \Gamma} (x - \Gamma s_c) \]  \hspace{1cm} (19)

where \( x^* \) is the corrected image after cloud removal. \( \Gamma s_c \) is a side product which represents various cloud contributions depending on their thickness at a subpixel level. This cloud retrieval result provides more detailed information than a binary mask file for cloud detection only. Specifically, cloud detection is achieved in the proposed cloud removal model after the cloud abundance is obtained. The fractional maps of the other materials are intermediate products as well. However, we mainly focus on cloud thickness in this paper.

The correction fails when \( \Gamma = 1 \). If \( \Gamma = 1 \), according to (14), \( x \approx s_c \). Applying (19), \( x^* = 0 \). This refers to the case of opaque clouds, which means that the underlying ground signal has been completely blocked. In this situation, reconstruction methods can be applied, e.g., by using multitemporal images to estimate the data of the blocked pixels [45]–[48]. In this paper, we focus on transparent thin cloud cases only.

## IV. Experimental Results

### A. Study Area and Data

To test the performance of the ST-SMA method, multispectral and hyperspectral images from the Landsat 8 OLI and EO-1 Hyperion, respectively, were used in our experiments. The details of the experimental images are summarized in Table I.

1) Landsat 8 OLI Data: Landsat 8 OLI multispectral images contain eight spectral bands with a spatial resolution of 30 m. The study areas selected from OLI were in Australia encompassing three typical landscapes with different types of clouds.

Validation of the performance of a cloud removal approach is not an easy task since there is no ground reference in the simultaneous atmospheric conditions. Fortunately, OLI captures a new spectral band (Band 9) at wavelengths ranging from 1.36 \( \mu \text{m} \) to 1.38 \( \mu \text{m} \) for detecting cirrus clouds. This narrow band has a strong ability to identify water vapor absorption and cirrus signal scattering [12], [49]. Cirrus cloud will appear bright in this band while sunlight reflected from the land’s surface will be entirely absorbed. Hence, this band is advantageous for cirrus cloud detection. This cirrus band with center wavelengths at 1.375 \( \mu \text{m} \) was used to validate the cloud detection results in this study.

2) EO-1 Hyperion Data: The Hyperion hyperspectral data were collected by the EO-1 satellite which was launched in November 2000. Hyperion images contain 242 spectral bands with wavelengths from 400 nm to 2500 nm with 30-m spatial resolution. The first 70 bands cover the visible/near-infrared region, and the bands from 71 to 242 cover the shortwave-infrared region. Level 1R data downloaded from the USGS website (http://earthexplorer.usgs.gov/) gave radiometrically corrected images which were used in this study. A subset of the Hyperion data with 122 bands was kept after calibration and noisy band removal. The Hyperion test data were selected in the Lulea region in Sweden as scene 4 showed in Table I. The water area is Lulealven river in the east of Sweden.

We also selected cloud free images from the closest date to each scene from the USGS website (http://earthexplorer.usgs.gov/) and used them to assess the quality of the corrected data. We assume that little change happened in the period between the two acquisition dates and only the atmospheric condition was different between the cloudy and cloud-free images. The images tested in the study were of size 400 \( \times \) 400 pixels for the OLI image and 1000 \( \times \) 256 pixels for Hyperion data. Image normalization was performed by converting the raw digital number to top-of-atmosphere reflectance ranging from 0 to 1.

<table>
<thead>
<tr>
<th>Scene</th>
<th>Path/Row</th>
<th>Acquisition date</th>
<th>Sensor</th>
<th>Cloud cover type</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>80/85</td>
<td>2013-9-9</td>
<td>OLI</td>
<td>Presence of moderate cloud, relatively thin with several patches of thick cloud.</td>
</tr>
<tr>
<td>2</td>
<td>86/72</td>
<td>2014-1-26</td>
<td>OLI</td>
<td>Thin cloud distributed over river, forest and grassland.</td>
</tr>
<tr>
<td>3</td>
<td>89/83</td>
<td>2014-3-13</td>
<td>OLI</td>
<td>Relatively thick cloud cover in left area of image within large region of water body.</td>
</tr>
<tr>
<td>4</td>
<td>193/14</td>
<td>2013-8-26</td>
<td>Hyperion</td>
<td>Thin cloud cover over Lulea urban region and Lulealven river.</td>
</tr>
</tbody>
</table>
In general, it can reduce scene-to-scene variability. Within the data set, the shape of the solar spectrum was compensated to enhance the spectral differences between the cloud spectrum and other endmembers [50].

B. Cloud Thickness Extraction

Cloud thickness can be obtained by solving the unmixing problems in our cloud removal model. Due to different atmospheric conditions, solar angles, and cloud cover in different dates and locations, the cloud endmember was extracted from each cloudy image separately based on (10).

Fig. 4 illustrates the spectral reflectance of the cloud endmember (solid line) for scene 1. Following the selection of the cloud endmember, the other three endmembers were retrieved from land ground pixels using the VCA method [43]. VCA is an EEA which assumes the presence of pure pixels, and it is effective and applicable for our cases. In the VCA algorithm, endmembers are presented as the vertices of a simplex and their selection are achieved by iteratively projecting to orthogonal directions in a subspace projection of an initially determined endmember. The iterative process stops when a predefined number of endmembers is extracted. Fig. 4 shows the spectra of three distinct materials identified in scene 1. Accordingly, ten endmembers were extracted for the Hyperion scene 4. Cloud thickness $\Gamma$ was obtained by solving (14) with the constraints as discussed in the previous section.

Cloud detection and removal were also performed using the HOT method [21]. Fig. 5 shows the original image, cloud detection results using the proposed method ST-SMA and the HOT method, and the corresponding cirrus band for the OLI scenes. The value of a pixel in the cloud detected image represents the thickness of cloud. We can see that HOT method provides good performance for scene 1 as shown in Fig. 5(c), but poorer performance for scenes 2 and 3 as shown in Fig. 5(g) and (k) where some background features appear, especially for large water bodies. Our method performs much better as shown in Fig. 5(d), (h), and (l). For the purpose of quantitatively validating the cloud detection results, scatterplots of the cloud detection results versus the cirrus band were generated and are shown in Fig. 7. The correlation coefficient between cloud thickness derived by the ST-SMA and the cirrus band data is 0.939, 0.801, and 0.939 for the three scenes, respectively, whereas the correlation coefficient obtained by the HOT methods was 0.844, 0.781, and 0.721, respectively. This quantitative assessment also shows that the proposed method performs better than the HOT method for all the OLI scenes.

C. Cloud Correction Results

In this set of experiments we assess the quality of the corrected images by comparing it with reference images. (19) was applied to conduct the cloud removal for the four scenes using the cloud thickness estimated in the earlier step. Figs. 6 and 8 show the original images, the reference images, and the corrected images of OLI and Hyperion data, respectively. From a qualitative point of view, we can see from Fig. 6 that the proposed method works effectively for various backgrounds with different land covers and cloud types. When the cloud is relatively thick and the ground cover underneath the cloud has high reflectance, the HOT method over-corrected the images while our method could clearly restore the land features. Fig. 8 reveals a good visual result of the corrected Hyperion image using ST-SMA method. The thin clouds over the whole scene have been effectively removed. The execution time of the proposed method on an EO-1 Hyperion subset is less than one second for 1000 pixels with 122 bands on a PC with an Intel® Core i7-3770 CPU at 3.4 GHz, 64-bit Operating System. The total execution time for the full scene is about 5 min, which can be reduced if a better CPU and code optimized for speed is used.

A comparison of spectral profile from cloudy, corrected, and reference images is selected as another validation approach. Fig. 9 depicts the spectral profiles of vegetation, water, and soil areas before and after the correction using the ST-SMA and HOT methods, respectively, as well as the reference data for scene 1. These profiles show the mean values of 10 randomly selected regions in the cloud cover areas. We can see that the spectral profile of corrected image by ST-SMA has a more similar shape with the profile from the reference image when compared with the HOT method. Fig. 9 also illustrates that the ST-SMA cloud removal method does not change the spectral properties of original data.

We also applied the spectral angle mapper (SAM) [51] to quantitatively evaluate the similarity between the cloudy (or corrected) spectra and the reference spectra. If a spectrum $s(n), n = 1, 2, \ldots, N$ is treated as a vector $\mathbf{s}$ in which $N$ is the number of bands. The SAM measures the spectral angle between $\mathbf{s}_1$ and $\mathbf{s}_2$ by calculating the arccosine of the normalized dot product of the spectra using

$$\alpha = \cos^{-1} \left( \frac{\mathbf{s}_1 \cdot \mathbf{s}_2}{\|\mathbf{s}_1\| \|\mathbf{s}_2\|} \right)$$

$$= \cos^{-1} \left( \frac{\sum_{n=1}^{N} s_1(n)s_2(n)}{\left( \sum_{n=1}^{N} s_1^2(n) \right)^{\frac{1}{2}} \left( \sum_{n=1}^{N} s_2^2(n) \right)^{\frac{1}{2}}} \right).$$

(20)

Smaller angles indicate higher similarity, although the magnitude of the vectors can be different. The SAM results of Fig. 9(a) were 0.254 (cloudy versus reference), 0.136 (HOT versus reference), and 0.086 (ST-SMA versus reference), respectively.
Fig. 5. Comparison of cloud detection results for the OLI data. (a) Original image-scene 1. (b) Cirrus band-scene 1. (c) HOT results-scene 1. (d) ST-SMA results-scene 1. (e) Original image-scene 2. (f) Cirrus band-scene 2. (g) HOT results-scene 2. (h) ST-SMA results-scene 2. (i) Original image-scene 3. (j) Cirrus band-scene 3. (k) HOT results-scene 3. (l) ST-SMA results-scene 3.

Fig. 6. Cloud removal results and reference images of OLI data (R = band 5, G = band 4, B = band 3). (a) Cloudy image-scene 1. (b) HOT-scene 1. (c) ST-SMA-scene 1. (d) Reference image-scene 1. (e) Cloudy image-scene 2. (f) HOT-scene 2. (g) ST-SMA-scene 2. (h) Reference image-scene 2. (i) Cloudy image-scene 3. (j) HOT-scene 3. (k) ST-SMA-scene 3. (l) Reference image-scene 3.
Fig. 7. Scatterplots of HOT results and ST-SMA results versus cirrus band values for the multispectral scenes. (a) Scene 1. (b) Scene 1. (c) Scene 2. (d) Scene 2. (e) Scene 3. (f) Scene 3.

Fig. 8. Cloud removal results and reference images of Hyperion data (R = band 49, G = band 29, B = band 20). (a) Cloudy image-scene 4. (b) ST-SMA-scene 4. (c) Reference image-scene 4.

Fig. 9. Spectral profile of mean value from ten polygon samples in the cloud cover areas for cloudy, corrected and reference images for scene 1. (a) Vegetation. (b) Water. (c) Soil.

respectively. Accordingly, results of Fig. 9(b) and (c) are 0.242, 0.211, 0.156 and 0.136, 0.103, 0.05, respectively. The lowest SAM values, 0.086, 0.156, and 0.05, indicate that the shape of the corrected spectra using ST-SMA is the closest to the reference spectra.

Table II provides detailed $R^2$ results of the cloudy and corrected images versus reference images, band by band, for the three OLI scenes. We can see that the $R^2$ value of corrected versus reference images is much higher than cloudy versus reference images in coastal aerosol and visible bands. This is due to the strong effects of cloud cover in these bands. In near-infrared and shortwave infrared bands, the $R^2$ value of corrected versus reference images improved slightly since the cloudy and reference images already have relatively high agreement. Between the two methods implemented on OLI images, the
TABLE II
LINEAR REGRESSION MODEL OF CLOUDY AND CORRECTED IMAGES BY THE ST-SMA AND HOT METHODS VERSUS REFERENCE IMAGES OVER ALL CLOUDY PIXELS

<table>
<thead>
<tr>
<th>Scene</th>
<th>Cloudy</th>
<th>HOT</th>
<th>ST-SMA</th>
<th>Cloudy</th>
<th>HOT</th>
<th>ST-SMA</th>
<th>Cloudy</th>
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<th>Cloudy</th>
<th>HOT</th>
<th>ST-SMA</th>
<th>Cloudy</th>
<th>HOT</th>
<th>ST-SMA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Band 1</td>
<td>0.233</td>
<td>0.337</td>
<td>0.798</td>
<td>0.281</td>
<td>0.781</td>
<td>0.802</td>
<td>0.356</td>
<td>0.458</td>
<td>0.469</td>
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<td></td>
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<tr>
<td>Band 2</td>
<td>0.271</td>
<td>0.534</td>
<td>0.834</td>
<td>0.383</td>
<td>0.824</td>
<td>0.844</td>
<td>0.624</td>
<td>0.523</td>
<td>0.587</td>
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<tr>
<td>Band 3</td>
<td>0.383</td>
<td>0.602</td>
<td>0.856</td>
<td>0.611</td>
<td>0.879</td>
<td>0.896</td>
<td>0.648</td>
<td>0.712</td>
<td>0.715</td>
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<tr>
<td>Band 4</td>
<td>0.434</td>
<td>0.723</td>
<td>0.845</td>
<td>0.752</td>
<td>0.887</td>
<td>0.913</td>
<td>0.566</td>
<td>0.635</td>
<td>0.641</td>
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<td>Band 5</td>
<td>0.452</td>
<td>0.719</td>
<td>0.792</td>
<td>0.881</td>
<td>0.896</td>
<td>0.925</td>
<td>0.655</td>
<td>0.635</td>
<td>0.728</td>
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<td>Band 6</td>
<td>0.381</td>
<td>0.719</td>
<td>0.874</td>
<td>0.892</td>
<td>0.912</td>
<td>0.928</td>
<td>0.575</td>
<td>0.635</td>
<td>0.749</td>
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<tr>
<td>Band 7</td>
<td>0.805</td>
<td>0.875</td>
<td>0.896</td>
<td>0.896</td>
<td>0.923</td>
<td>0.935</td>
<td>0.653</td>
<td>0.712</td>
<td>0.788</td>
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</tr>
</tbody>
</table>

ST-SMA method outperforms the HOT method consistently. The normalized difference vegetation indices (NDVI) of the cloudy and corrected Hyperion images were also compared. From the scatterplots in Fig. 10, the corrected image using ST-SMA method has higher $R^2$ value (0.718) than the cloudy image (0.456). The corrected images are expected to be valuable for classification and target detection.

While snow can be confused with clouds in the visible bands, they have different spectral profiles in other bands [52]. In our proposed cloud removal method, snow is treated as a unique endmember like other ground cover types. Fig. 11 shows the cloud removal results of an image with both snow and cloud cover. Fig. 11(a) and (b) are the original image and the corrected image, respectively. We can see that the cloud effect is removed, while snow is still present.

V. DISCUSSIONS AND CONCLUSIONS

In this paper, we have developed a new method, called ST-SMA, for cloud thickness detection and cloud removal in optical remote sensing imagery. ST-SMA makes joint use of atmospheric scattering theory and linear spectral mixture analysis to describe the effects of cloud on the reflectance from underlying land. The approach is based on the assumption that there is a linear relationship between cloud thickness and spectral reflectance. Energy absorption is also considered in the solar radiation propagation model. Cloud saturation is not considered in this study given that we focus on thin cloud removal. A concept of pure cloud is introduced in this paper, and we propose to extract a cloud spectrum by searching for the pixels with the maximum total energy in all the spectral bands in each cloud-affected image. A modified version of fully constrained linear spectral unmixing was applied to estimate cloud thickness, which is equivalent to cloud abundance. Cloud thickness is presented for each pixel instead of binary masking only. This represents a novel contribution for cloud detection and removal by combining physical modeling and mixture analysis. The proposed method has no requirement for meteorological data and does not rely on reference images.

The screening results of multispectral data were visually and quantitatively compared with the cirrus band of the Landsat OLI sensor. Validation of the cloud removal algorithm was conducted for OLI and Hyperion data by comparing corrected images with reference images through scatter plots and $R^2$ values and spectral similarity evaluation with SAM. The HOT method was also implemented in the experiments. The testing results demonstrate that our method ST-SMA provides better performance than the HOT method and can provide cloud free images with high quality.

The cloud removal performance is sensitive to some parameters in the proposed method. First and foremost, the cloud endmember should be selected in regions containing the thickest cloud. This is not a difficult issue in practice since it is very easy to find these areas in optical images. Second, the number of endmembers needs to be smaller than the number of spectral bands to make the least squares solution reliable. For correction of Landsat 8 images, the proposed method is mainly suitable for simple landscapes, containing three or four endmember classes only. For complicated scenes, such as urban areas, the ST-SMA method can be applied to hyperspectral images where the number of bands can be over two hundred. Alternatively, the pixel-adapted subset of endmembers can be used in unmixing. The conventional approach is to find all the endmembers present in the whole image and unmix each pixel into the complete set of endmembers. More efficient methods have been developed to estimate a subset of endmembers for which individual pixels are associated with first, and the unmixing is then conducted adaptively for each pixel [53], [54]. In this way, the number of potential endmembers for each particular pixel is often reduced to 3 or 4, and this allows, to some extent, the use of spectral unmixing techniques with multispectral data.

Extra computational load is introduced by the nonlinear least squares problem involved in ST-SMA; however, it is not a serious issue as cloud removal is an off-board post-processing task. Cloud shadow is difficult to model and it is not addressed in this paper since it is not as relevant when we focus on thin cloud contaminated image restoration.
In our future work, the cirrus band will be considered to assist with the cloud detection. Wider testing will be conducted, for example, on the case of cloud contamination over snow, which presents relevant challenges. The corrected images will also be further processed for various applications.

ACKNOWLEDGMENT

The authors would like to thank the Editors and the anonymous reviewers for their outstanding comments and suggestions, which greatly helped us to improve the technical quality and presentation of our manuscript.

REFERENCES


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Dr. Jia is an Editor of the Annals of GIS and an Associate Editor of the IEEE TRANSACTIONS ON GEOSCIENCE AND REMOTE SENSING.