MATH 251 (Fall 2009) Hwk on Lines and Planes (10.5)

Recall the following defintions from class:

- (i) A **vector parametrization** of the line through the endpoint of the vector **a** in the direction of the vector **b** is given by $\mathbf{r}(t) = \mathbf{a} + t\mathbf{b}$, where $t \in \mathbf{R}$.
- (ii) A scalar parametrization of the line in (i) is

$$x = a_1 + tb_1$$
$$y = a_2 + tb_2$$
$$z = a_3 + tb_3$$

where $\mathbf{a} = (a_1, a_2, a_3)$ and $\mathbf{b} = (b_1, b_2, b_3)$.

- (iii) A **level set equation** of a plane is an equation of the form ax + by + cz = d, where a, b, c, d are real numbers.
- (iv) A **parametrization** of a plane through the endpoint of the vector \mathbf{u} that contains the vectors \mathbf{v} and \mathbf{w} is of the form $\mathbf{r}(s,t) = \mathbf{u} + s\mathbf{v} + t\mathbf{w}$, where $s,t \in \mathbf{R}$.
- (1) Find a vector parametrization and a scalar parametrization for the line passing through the point (3, -4, 5) in the direction of the vector $\mathbf{v} = -2\mathbf{i} + 7\mathbf{j} + 3\mathbf{k}$.
- (2) Find a vector parametrization for the line passing through the points (1,2,3) and (9,8,7).
- (3) Find a vector parametrization for the line through the point (2,5,6) and perpendicular to the plane 2x 4y + 5z = 9.
- (4) Find a vector parametrization for the line through the point (2, 5, 6) and parallel to the line with scalar parametric equations x = -1 2t, y = 3t + 7, z = 6t 2.
- (5) Find the level set equation and a parametrization of the plane through the point (1, 2, 3) with normal vector (4, 5, 6).
- (6) Find the level set equation of the plane through the point (1, 2, 3) parallel to the plane 3x 5y + 7z = 8.

- (7) Find the level set equation and a parametrization of the plane through the points (1,0,-1), (3,3,2), and (4,5,-1).
- (8) Find a parametrization of the plane that contains both the point (2, 4, 6) and the line x = 7 3t, y = 3 + 4t, z = 5 + 2t.
- (9) Does the line $x=3+2t,\ y=6-5t,\ z=2+3t$ intersect the plane 3x+2y-4z=1?