## MATH 251 (Spring 2004) Diagnostic Quiz

This quiz does not count towards your grade. No books, notes, or friends! Show all work. Use extra paper if you need!
(1) Let $f(x)=x^{2}$.
(a) Compute $f^{\prime}(3)$
(b) What is the definition of $f^{\prime}(3)$ ?
(c) What does $f^{\prime}(3)$ mean geometrically?
(2) Find (a) $\int_{1 / 2}^{2} \frac{1}{x} d x$
(b) $\int_{0}^{\infty} x e^{-x^{2}} d x$
(3) On what intervals is $f(x)=x^{3}-3 x^{2}+7 x$ increasing?
(4) State the Fundamental Theorem of Calculus.
(5) Let $f(x)=\int_{5}^{x} \sin \left(t^{3}\right) d t$. What is $f^{\prime}(10)$ ?

