Pansharpening via Detail Injection Based Convolutional Neural Networks

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Abstract—Pansharpening aims to fuse a multispectral (MS) image with an associated panchromatic (PAN) image, producing a composite image with the spectral resolution of the former and the spatial resolution of the latter. Traditional pansharpening methods can be ascribed to a unified detail injection context, which views the injected MS details as the integration of PAN details and bandwise injection gains. In this paper, we design a new detail injection based convolutional neural network (DiCNN) framework for pansharpening with the MS details being directly formulated in end-to-end manners, where the first detail injection based CNN (DiCNN1) mines MS details through the PAN image and the MS image, and the second one (DiCNN2) utilizes only the PAN image. The main advantage of the proposed DiCNNs is that they provide explicit physical interpretations and can achieve fast convergence while achieving high pansharpening quality. Furthermore, the effectiveness of the proposed approaches is also analyzed from a relatively theoretical point of view. Our methods are evaluated via experiments on real MS image datasets, achieving excellent performance when compared to other state-of-the-art methods.

Index Terms—Convolutional neural networks (CNNs), detail injection, pansharpening.

I. INTRODUCTION

Due to the physical characteristics of multispectral (MS) image sensors, they generally acquire MS images with limited spatial resolution. However, high spatial resolution MS images are required in many applications, such as classification, target detection, scene interpretation, and spectral unmixing [1], [2]. Therefore, pansharpening has been an active area of research, drawing significant attention in the area of remotely sensed image processing. The pansharpening task aims at fusing a low spatial resolution MS image and a registered wide-band panchromatic (PAN) image, utilizing the detail information contained in the PAN image to sharpen the MS image, hence yielding a high spatial resolution MS image [1]. The task can be seen as a special reconstruction based on different types of data with different characteristics. For simplicity, low spatial resolution MS images are called LRMS images, and high spatial resolution MS images are called HRMS images, hereinafter. A HRMS image pansharpened from the LRMS image is called pansharpened HRMS image hereinafter. Ideally, as a full resolution image, the pansharpened HRMS image should have the same spectral resolution as the original LRMS image and the same spatial resolution as the corresponding PAN image.

Over the past decades, a wide variety of pansharpening methods have been proposed in the literature [1]–[4]. Among such existing methods, component substitution (CS) and multi-resolution analysis (MRA) are two widely representative categories [1]–[3]. CS approaches usually replace certain components of the MS image with those from the PAN image in a given domain, which include principal component analysis based pansharpening [5]–[7], Brovey transform based pansharpening [8], [9], and Gram–Schmidt (GS) transform based pansharpening [10], [11], among others. In contrast, MRA methods exploit the spatial information via a multiresolution decomposition of the images, which generally involves detail extraction and detail integration in multiple scales. Examples are pansharpenings based on decimated wavelet transform [12], undecimated wavelet transform [13], a trous wavelet transform (ATWT) [14]–[16], and Laplacian pyramid [17]–[19]. The aforementioned methods differ mainly in how spatial details are extracted from the PAN image and how they are injected into the pre-interpolated LRMS image. One major challenge for CS/MRA approaches is to preserve spatial details resolved from the PAN image as much as possible, while avoiding spectral distortion. This refers to the spectral deviation from an ideal spectrum,
especially when PAN and MS images are acquired in spectral ranges that overlap only partially [1], [20]. Unfortunately, existing CS/MRA methods are often prone to significant spectral distortion [3], even under some improvement of fusion strategies such as histogram matching [21], weighted detail injection [16], or some hybrid intermediate processes [22]. This is probably due to the fact that the details are not very effectively learned and injected, although CS/MRA approaches indeed aim to utilize the detail information.

Recently, convolutional neural networks (CNNs) start prevailing in image enhancement tasks such as super-resolution [23], [24] and pansharpening [20], [25]. Super-resolution is, to some degree, a pansharpening-related task, as both super-resolution and pansharpening aim to enhance image resolution. There are, however, some differences among them since the former is usually a single input single output (SISO) case. Dong et al. proposed a super-resolution CNN (SRCNN), which is a three-layer CNN, to learn the mapping from the input low-resolution image to the output high-resolution image [23]. Kim et al. designed a deep CNN structure for super-resolution, where the residual component is learned [26]. Whether or not details are injected from the PAN image to its associated LRMS image represents the major difference between pansharpening and super-resolution tasks. Considering this, Masi et al. presented a pansharpening CNN (PNN) following the basic thread of SRCNN [20], where the pre-interpolated LRMS image is stacked with the PAN image at the input layer, and then a CNN process is used to learn the relationship between the input and the pansharpened HRMS image. Although PNN exhibits good performance on real remotely sensed data, difficulties arise from the long-time training iterations and the problem that it misses the domain-specific pansharpening structure and roughly treats pansharpening as a black-box learning procedure. Afterwards, Wei et al. designed a CNN method for pansharpening [25]. The method comprises the process of residual learning and the subsequent dimension reduction, which is faced with the problems that the learned residual has no explicit physical interpretation for pansharpening and there is an additional computation load related to dimension reduction. They also introduce strategies such as multiscale kernels into the CNN-based pansharpening [27].

In this paper, a general detail injection formulation, namely, detail injection based CNNs for pansharpening (DiPAN), is summarized, which is able to accommodate CS/MRA pansharpening methods. The proposed DiPAN can be used as a domain-specific structure to guide the design of new pansharpening methods. In the context of our DiPAN framework, two detail injection based CNNs (DiCNNs) for MS detail learning are introduced, where the main contributions of this paper can be summarized as follows.

1) The first method, called DiCNN1, adopts a framework in which the pathway of stacked convolutional layers only learns the MS details from the combination of the pre-interpolated LRMS image and the PAN image in an end-to-end manner, resulting in good initialization. DiCNN1, following the basic idea in our previous work [28], has clear interpretability in the detail injection context, and can greatly reduce the uncertainty of learning, thus achieving high computational efficiency and pansharpening quality. A detailed description of the method, followed by a discussion and extensive experimental results, are provided in this paper. Furthermore, we present a theoretical analysis and proof of the effectiveness of DiCNN1. To the best of our knowledge, the effectiveness of a pansharpening CNN has not been previously explored from such a theoretical point of view.

2) The second method, called DiCNN2, is capable of transfer learning when there are bad bands in test MS images. DiCNN2 works under the assumption that ideal MS detail is only relevant to the PAN image, and directly uses the PAN image as the input of the convolutional layer pathway, which makes it able to perform transfer learning in addition to the regular pansharpening task. Since its input is a one-dimensional (1-D) PAN image only (with a small amount of CNN free parameters), DiCNN2 yields very fast computation.

The remainder of the paper is organized as follows. Section II introduces the detail injection framework. Section III summarizes major existing CNN-based super-resolution and pansharpening methods. Section IV introduces our detail injection based CNN pansharpening methods and presents the corresponding complexity analysis. Section V evaluates the proposed methods via experiments with real MS datasets. Section VI concludes the paper with some remarks and hints at plausible future research lines.

II. DETAIL INJECTION FRAMEWORK

Let $\mathbf{P} \in \mathbb{R}^{H \times W}$ denote an observed PAN image with size $H \times W$; let $\mathbf{M} \in \mathbb{R}^{H \times W \times N_b}$ be a pre-interpolated LRMS, which has been interpolated spatially to the scale of the PAN image (with $N_b$ being the number of bands); and let $\tilde{\mathbf{M}}$ be the pansharpened HRMS image.

Traditionally, CS/MRA methods are viewed as two major groups of pansharpening methods [1]. CS category can be generally formulated as

$$\tilde{M}_b = \bar{M}_b + g_b \cdot (P - I_c), \quad b = 1, \ldots, N_b$$

(1)

where $\bar{M}_b$ and $\bar{M}_b$ are the $b$th bands of $\tilde{M}$ and $\bar{M}$, respectively, $g_b$ represents the injection gain associated with $\bar{M}_b$, $N_b$ is the number of MS bands, and $I_c$ is the intensity component of the MS image, which is often a weighted sum $I_c = \sum_{b=1}^{N_b} \omega_b \tilde{M}_b$. To show the substitution process in CS methods, (1) can be reformulated as

$$\tilde{M}_b = \bar{M}_b - I_c + g_b \cdot (P - I_c) + I_c$$

$$= (\tilde{M}_b - I_c) + g_b \cdot (P - g_b^{-1} I_c)$$

(2)

which suggests that, in a CS method, the component $I_c$ is substituted with the component $g_b \cdot (P - g_b^{-1} I_c)$. On the other hand, the general formulation of MRA methods is of the form [1]

$$\tilde{M}_b = \bar{M}_b + g_b \cdot (P - P_c), \quad b = 1, \ldots, N_b$$

(3)
Fig. 1. Schematic diagram of the DiPAN framework.

where $P_c$ denotes the low-frequency component of the PAN image, which is usually obtained in a MRA way. According to the representations in (1) and (3), both CS and MRA methods are normally based on two sequential phases: First, the extraction of MS details from the PAN image, which usually comprises intermediate processes, such as yielding PAN details and obtaining band injection gains. Second, the injection of the MS details into the LRMS image to produce the HRMS image. Therefore, such two categories of pansharpening methods can be represented in a unified detail injection framework, namely DiPAN, as follows:

$$\hat{M}_b = \tilde{M}_b + g_b \cdot d$$

where $d$ represents the PAN details, which are usually calculated by involving both the PAN image and the MS image with a certain criterion, $D_b = g_b \cdot d$ denotes the MS details, which should complement the pre-interpolated LRMS image $\tilde{M}$, while $g_b$ stands for the associated injection gain responsible for transferring the PAN details to the MS details. A schematic diagram of DiPAN is given in Fig. 1, where it is indicated that the full-resolution pansharpened HRMS image $\hat{M}$ can be decomposed into the MS details and the LRMS approximation.

As the formulation in (4) and the schematic diagram in Fig. 1 indicate, DiPAN has clear physical interpretability for the pansharpening process, which can be used as a pansharpening domain-specific structure to guide the design of new pansharpening methods.

III. SUPER-RESOLUTION AND PANSHARPENING USING CNN STRATEGY

Recently, CNNs were successfully applied in image super-resolution and pansharpening. CNNs are usually treated as the descendants of traditional artificial neural networks [29]–[31], in which assumptions such as a limited receptive field (processing input only in a neuron’s local neighborhood) and the spatial invariant weight (so-called weight sharing) are normally jointly employed.

The response of a convolutional layer in a CNN can be given by

$$Y_l = \varphi(W_l \ast X_l + B_l)$$

where $\ast$ denotes the convolution operation, $X_l$ and $Y_l$ are the input and output of the $l$th layer, respectively, $W_l$ and $B_l$ are the weight and bias metrics, respectively, and $\varphi(\cdot)$ represents the activation function. Due to its ability to mitigate gradient vanishing and its computational simplicity, the rectified linear unit (ReLU) [32] is commonly used in CNNs, whose input-output relation is $Y_l = \max(0, X_l)$ [23], [33]–[35].

Both image super-resolution and pansharpening intend to recover high-resolution images from the observed low-resolution data, with the major disparity being that one is a SISO process and the other one is a MISO one. In image super-resolution, usually the low spatial resolution image (as a single input) is processed to output a high spatial resolution image, while pansharpening utilizes the MS image with low spatial resolution and the PAN image with low spectral resolution as two separate data sources to recover the full resolution HRMS image. The two kinds of image resolution enhancements mentioned above are used as mathematical tools to minimize the loss function of expected square error as

$$\ell(\theta) = E\|\hat{H}(X; \theta) - Y\|_F^2$$

where $\hat{H}$ is the predicted high-resolution image following a parametric structure, $Y$ is the ideal high-resolution image, $\theta$ denotes the parameters used to infer the predicted image, and $X$ is the low-resolution input, which means a low spatial resolution image for image super-resolution that represents both the low spectral resolution PAN image and the associated LRMS image for pansharpening.

Dong et al. designed a three-layer CNN for image super-resolution able to directly learn the mapping between the low-resolution image and the high-resolution image, which is called super-resolution CNN (SRCNN) [23]. Therein patch extraction and representation are used to improve computational efficiency and feature locality in the training phase. The objective is to
minimize the following patchwise mean square error:

\[
\ell(\theta) = E\|\hat{H}(X; \theta) - Y\|_F^2
\]

\[
= \frac{1}{N_p} \sum_{i=1}^{N_p} \|\hat{H}^{(i)}(X^{(i)}; \theta) - Y^{(i)}\|_F^2
\]

(7)

where \(i\) is the index of patches, \(N_p\) denotes the number of total patches, \(\theta\) represents the free CNN parameters to be optimized under the CNN context, \(X^{(i)}\) refers to the \(i\)th patch in the low-resolution image, and \(\hat{H}^{(i)}\) stands for the \(i\)th patch in the predicted high-resolution image. As a counterpart for pansharpening purposes, Masi \textit{et al.} introduced a PNN [20], which stacks the pre-interpolated LRMS image and the PAN image together and then uses a CNN to mine the mapping between this concatenation and a real HRMS image.

The loss function to be minimized is

\[
\ell(\theta) = E\|\hat{M}(G; \theta) - Y\|_F^2
\]

\[
= \frac{1}{N_p} \sum_{i=1}^{N_p} \|\hat{M}^{(i)}(G^{(i)}; \theta) - Y^{(i)}\|_F^2
\]

(8)

where \(G = (\hat{M}, P)\) in the size \(H \times W \times (N_0 + 1)\) denotes the concatenation of the pre-interpolated LRMS image \(\hat{M}\) and the PAN image \(P\) along the band dimension. Here, the target \(Y\) stands for the ideal HRMS for the pansharpening case. Considering that MS images are in 3-D data arrangement, \(\hat{M}\) and \(Y\) are originally three-way or third-order tensors [36]. To accommodate a matrix representation, \(\tilde{M}\) and \(Y\) in (8) are unfolded as matrices, for example, along the first mode and being denoted as \(\tilde{M}^{(1)}\) and \(Y^{(1)}\) [36]. But, for simplicity, \(\tilde{M}\) and \(Y\) in (8) represent their unfolding matrices \(\tilde{M}^{(1)}\) and \(Y^{(1)}\), respectively. If not stated otherwise, the remainder of the paper follows the same expression routine when involving three-way tensor representations.

The deep residual network (ResNet) has reached excellent performance in image classification [37]. Its success largely stems from attaching an identity skip connection to fit a residual mapping. Kim \textit{et al.} extended ResNet and proposed a deep network for super-resolution purposes, which intends to learn the residual supplementary to the input low-resolution image instead of the predicted high-resolution image itself [26]. The loss function is defined as follows:

\[
\ell(\theta) = E\|\hat{R}(X; \theta) + X - Y\|_F^2
\]

\[
= \frac{1}{N_p} \sum_{i=1}^{N_p} \|\hat{R}^{(i)}(X^{(i)}; \theta) + X^{(i)} - Y^{(i)}\|_F^2
\]

(9)

where \(R\) represents the residual that needs to be learnt. Later, Wei \textit{et al.} used a similar strategy for pansharpening, termed deep residual pansharpening neural network (DRPNN) [25]. In the DRPNN, the concatenation of the pre-interpolated LRMS image and the PAN image pass through both stacked layers and a shortcut connection to yield the residual and, then, an additional convolutional layer is included for dimensionality reduction.

The connected objective is to minimize the following loss:

\[
\ell(\theta) = \|\omega(\hat{R}(G; \theta) + G) - Y\|_F^2
\]

\[
= \frac{1}{N_p} \sum_{i=1}^{N_p} \|\omega(\hat{R}^{(i)}(G^{(i)}; \theta) + G^{(i)}) - Y^{(i)}\|_F^2
\]

(10)

where \(\omega(\cdot)\) denotes a convolution operation for dimensional matching.

In comparison with the CS/MRA approaches, CNNs provide a new possibility to perform learning for pansharpening, where the details are driven from the context. However, in comparison with DiPAN, the main limitation of the aforementioned CNN-based pansharpening approaches is the lack of physical interpretability, and the fact that they do not use an appropriate domain-specific structure. The weaknesses are, specifically, as follows.

1) PNN treats pansharpening merely as a black-box learning procedure, without considering the domain-specific structure useful to pansharpening, which results in a heavy training process and limited learning ability.

2) DRPNN involves the structure of residual and the subsequent dimension reduction, which faces the problem that the processed residual has no explicit physical interpretation in a pansharpening context, and there is additional computational burden for the dimension reduction step.

IV. PROPOSED METHODS

Based on the DiPAN framework in Section II, we develop DiCNNs for pansharpening. The advantages of the proposed DiCNNs can be summarized as follows.

1) We take into consideration the detail structure used in traditional CS/MRA-based pansharpening and then directly learn MS details, without separating the PAN details and the connected gains. This allows us to circumvent the intermediate process needed to learn such two pieces of information individually, thus reducing the model uncertainty.

2) Compared to existing CNN-based pansharpening methods, our newly proposed methods have clear and meaningful interpretation in the context of detail injection and can also achieve excellent learning performance.

A. First Detail Injection Based CNN (DiCNN)

Following DiPAN, our pansharpening method focuses on reconstructing the MS details in a CNN manner. To achieve this goal, we build a feedforward neural network, where a shortcut connection skips three stacked convolutional layers and the output of the shortcut is added to the output of stacked layers to yield the predicted HRMS [as shown in Fig. 2(a)]. This network employs the concatenation of the pre-interpolated LRMS and the PAN images as the input. However, only the pre-interpolated LRMS is propagated through the shortcut connection. In this way, the stacked layers utilize the interaction of the pre-interpolated LRMS and PAN images to yield only the MS details that can further supplement the LRMS.
image in order to produce the pansharpened HRMS image. Specifically, our objective is to minimize the following loss function:

\[
\ell(\theta) = ||\tilde{D}(G; \theta) + \tilde{M} - Y||_F^2
\]

\[
= \frac{1}{N_p} \sum_{i=1}^{N_p} ||\tilde{D}^{(i)}(G^{(i)}; \theta) + \tilde{M}^{(i)} - Y^{(i)}||_F^2
\]

(11)

where \(\tilde{D}\) represents the MS details reconstructed with the input \(G\), the concatenation of the LRMS image and the PAN image, and the parameter \(\theta\).

Practically, pansharpening is an ill-posed problem, which means that many solutions exist for a given low-resolution input. This is mathematically connected to an underdetermined inverse problem, of which the solution is not unique. In theory, such a problem can be relieved by constraining the solution space with appropriate prior information, which influences the overall performance of pansharpening. Fig. 3 depicts the basic structure of several CNN-based methods, with Fig. 3(a) and (b) representing the PNN and DRPNN (mentioned previously) and Fig. 3(c) representing our DiCNN1. As we can observe, the PNN directly learns the mapping between its input (the pre-interpolated LRMS image plus the PAN image) and the reconstructed HRMS image, without involving any prior knowledge on structure, regarding pansharpening just as a black-box learning problem. In the DRPNN, a residual structure is introduced into pansharpening [as shown in Fig. 3(b)], motivated by the residual learning process for image super-resolution in [26]. However, this residual structure brings some inherent weaknesses when used for pansharpening. First, DRPNN uses the concatenation of the pre-interpolated LRMS image and the PAN image as its input. This input goes through the stacked layers and the shortcut connections simultaneously, which forces the output of stacked layers pathway to be of the same dimensionality as the input of the input concatenation, i.e., one dimension more than that of the pansharpened HRMS image, thus yielding a residual learning result that has no explicit physical interpretation in a pansharpening context. Second, this dimensionality mismatch has to rely on an extra convolutional layer, which apparently aggravates the computational burden.

Different from PNN and DRPNN, our DiCNN1 takes into consideration the structure of the detail injection framework. It uses the concatenation of the pre-interpolated LRMS image and the PAN image as the input of the stacked layers, whereas the shortcut connection inputs only the pre-interpolated LRMS image. This strategy makes the output of stacked layers pathway be the MS details that can directly supplement the pre-interpolated LRMS image to produce the HRMS image, which guarantees that this CNN is able to directly learn the MS details. This implies that DiCNN1 does introduce a domain-specific structure with meaningful interpretation, meanwhile excluding the additional computational burden. On the other hand, compared to the detail injection based CS and MRA methods, DiCNN1 learns only the MS details per se, avoiding to separately process the PAN details and the associated gains and, hence, reducing the model uncertainty.

B. Second Detail Injection Based CNN (DiCNN2)

When a PNN model has been trained, the test MS images may be changed; for example, bad bands may be present in the data. In this situation, can a PNN model be transferred to pansharpen those different kinds of test images?

As mentioned in previous sections, pansharpening utilizes the details mainly existing in the PAN image to supplement the LRMS image, so as to obtain the HRMS image. These details can be viewed as the result from a filtering process, where certain low-frequency components are filtered out [38], which is a common rule for pansharpening on various sorts of images. Under this rule, it therefore makes sense that, for a given CNN, different sets of parameters suitable for pansharpening different kinds of images have certain inherent connections. As a result, it is possible to use a pre-trained CNN model on a certain kind of images for pansharpening other kinds of images. This is actually a transfer learning process [39]. By closely inspecting Fig. 2(a), we can see that both the PAN image and the LRMS image are fed into the convolutional layers pathway, which indicates that the LRMS image will significantly affect the extraction of details when the type of the MS image varies and, thus, reduce the robustness of the model learning in the stack layers pathway. To address this issue, we have developed another PNN, called DiCNN2 [as shown in Fig. 2(b)]. In DiCNN2, only the PAN image is connected to the convolutional layers pathway, which removes the influence of the LRMS image on detail extraction. Though this may also reduce the specificity of details for certain kinds of MS images, the shortcut connection still inputs the
pre-interpolated LRMS image to force the convolutional layers pathway to learn only the information about the MS details. The objective function to be minimized for DiCNN2 is

\[
\ell(\theta) = \left\| \hat{\mathbf{D}}(\mathbf{P}; \theta) + \tilde{\mathbf{M}} - \mathbf{Y} \right\|_F^2
\]

\[
= \frac{1}{N_p} \sum_{i=1}^{N_p} \left\| \hat{\mathbf{D}}^{(i)}(\mathbf{P}^{(i)}; \theta) + \tilde{\mathbf{M}} - \mathbf{Y}^{(i)} \right\|_F^2.
\]

(12)

In real applications, once a CNN is trained, the network parameters in the convolutional layers pathway are fixed, except for those on the last layer. When a new kind of images are input, only this layer needs to be fine-tuned.

It is noteworthy that DiCNN2 is also a kind of detail injection based CNN. In addition to performing pre-training transfer, DiCNN2 can be seen as an alternative to DiCNN1 for usual pansharpening tasks, where the data for training and prediction come from the same sensors. Fig. 3(d) depicts the simplified structure of such a PNN, which suggests that DiCNN2 can provide similar benefits as DiCNN1, such as meaningful detail injection interpretation, high computational efficiency, and model simplification. Especially, DiCNN2 uses the PAN image as the input of the stacked convolutional layers, in contrast with the concatenation of the PAN image and multi-band LRMS image, thus leading to even higher computational efficiency than DiCNN1.

In summary, we developed DiCNNs, both of which exhibit the capacity to perform the regular pansharpening task. But they also differ in the following three main aspects.

1) DiCNN1 and DiCNN2 have different network structures. As it can be observed in Fig. 2(a) and (b), and Fig. 3(c) and (d), DiCNN1 inputs both the PAN image and the LRMS to the convolutional pathway, whereas DiCNN2 inputs only the PAN image to the convolutional pathway.

2) DiCNN1 and DiCNN2 are connected to different loss functions. This is because the different structures of the two CNNs lead to such different functions. Specifically, the loss function of DiCNN1 is given by (11), while that of DiCNN2 is given by (12). The convolutional kernels that need to be resolved in DiCNN1 are coupled with the concatenation of both the MS image and the PAN image, but in DiCNN2 those kernels are convolved only with the PAN image.

3) DiCNN1 and DiCNN2 can serve different purposes. Both DiCNN1 and DiCNN2 are able to perform the regular pansharpening task. However, DiCNN2 exhibits an additional ability to perform transfer learning. In DiCNN2, the LRMS image is separated out from the input of the convolutional pathway, which means that the bottom layer of the CNN’s convolutional pathway is not tightly relevant to it. Thus, for a test LRMS image with bad bands, we only need to fine-tune the top convolutional layer, which is a kind of transfer learning.

V. EXPERIMENTAL RESULTS

This section evaluates the performance of our pansharpening methods, where three real remotely sensed image datasets are considered. These datasets were acquired with WorldView-2, IKONOS, and Quickbird sensors. During the evaluation, we conduct reduced-resolution and full-resolution experiments, as well as transfer learning experiments.

In the case of reduced-resolution assessments, we set experiments using Wald’s protocol [40]. The MS image and the PAN image were degraded to a lower resolution by using a Gaussian filter with a factor of 4 [41], and then the degraded MS image was pre-interpolated to the same spatial size as the degraded PAN image using a polynomial kernel (EXP) [4]. The criteria used for the assessment include x-band extension of universal image quality index (Qx) [42], spatial correlation coefficient (SCC) [43], spectral angle mapper (SAM) [44], and Erreur Relative Globale Adimensionnelle de Synthèse (ERGAS) [45]. These indexes are widely used to measure the qualities of pansharpened images, with the original MS image as the ground-truth.
For fair comparison, we apply consistent parameter setting to different CNN-based pansharpening methods. Specifically, the number of convolutional layers in the convolutional pathway for all PNNs in comparison are set to be 3. Thus, we can compare the results under the basic network structure while avoiding the influence of the depthness of the hidden layers. In addition, each of them utilizes 64 filters with spatial size $3 \times 3$, except for the last layer with $N_6$ filters. Furthermore, all the training patches and validation patches are with the spatial size $41 \times 41$, totally being 25 600 patches, wherein 64 patches are randomly selected from training data as a mini-batch for SGD. The number of training iterations is set to $3 \times 10^5$ in all cases. The learning rate is initially set to 0.0001 and it adaptively updates based on Adam[46]. For CNN pansharpening, there are two major phases during the processing. In the first phase, the CNN model is solved with the training patches. In the second phase, the CNN model is used to pansharpen the MS image.

The learning properties of the compared CNN-based methods are summarized in Table I, which report our DiCNN1 and DiCNN2 built in pansharpening detail injection context. CNN-based pansharpening methods were trained using a GPU (Nvidia GTX 1060 3GB with CUDA 8.1 and CUDNN V5) through Caffe [47] in an Ubuntu 14.04 operating system, and tested on MATLAB R2016b via CPU mode (laptop with Intel I7 and 8GB RAM) through the deep learning framework Matconvnet [48] in Windows 10 operating system.

In addition to DiCNN1, DiCNN2, PNN, and DRPNN, several representative CS/MRA methods, including Gram Schmidt adaptive (GSA) [11], partial replacement adaptive component substitution (PRACS) [49], ATWT [16], band-dependent spatial-detail (BDSD) [50], and Generalized Laplacian pyramid with context-based decision (GLP-CBD) [2] are also tested for comparison. Notice that, there are no tricks, such as panmid with context-based decision (GLP-CBD) [2] are also tested. The best and second-best results are marked in bold and italic.

### Table I: Comparison Among CNN-Based Methods

<table>
<thead>
<tr>
<th></th>
<th>PNN</th>
<th>DRPNN</th>
<th>DiCNN1</th>
<th>DiCNN2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Detail Learning</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Residual Learning</td>
<td>No</td>
<td>Yes</td>
<td>No</td>
<td>No</td>
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<td>Transfer Learning</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
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### Table II: Quality Indexes of Different Pansharpening Methods Under a Reduced-Resolution Quality Assessment on a 256 × 256 Subscene of a Worldview-2 Dataset

<table>
<thead>
<tr>
<th>Method</th>
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<th>SAM</th>
<th>ERGAS</th>
<th>SCC</th>
<th>Time(s)</th>
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</thead>
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<td>EXP</td>
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<td>7.9558</td>
<td>8.0358</td>
<td>0.5127</td>
<td></td>
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<tr>
<td>GSA</td>
<td>0.9151</td>
<td>7.5830</td>
<td>4.3501</td>
<td>0.8973</td>
<td>0.85</td>
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<tr>
<td>PRACS</td>
<td>0.8682</td>
<td>7.3232</td>
<td>5.2048</td>
<td>0.8650</td>
<td>1.43</td>
</tr>
<tr>
<td>ATWT</td>
<td>0.8974</td>
<td>7.2241</td>
<td>4.7585</td>
<td>0.8926</td>
<td>0.84</td>
</tr>
<tr>
<td>BDSD</td>
<td>0.9178</td>
<td>8.1158</td>
<td>4.5293</td>
<td>0.8993</td>
<td>1.14</td>
</tr>
<tr>
<td>GLP-CBD</td>
<td>0.9148</td>
<td>7.5004</td>
<td>4.3438</td>
<td>0.8981</td>
<td>0.84</td>
</tr>
<tr>
<td>PNN</td>
<td>0.9243</td>
<td>7.6205</td>
<td>4.2924</td>
<td>0.8906</td>
<td>2.20</td>
</tr>
<tr>
<td>DRPNN</td>
<td>0.9325</td>
<td>7.1775</td>
<td>3.9064</td>
<td>0.9149</td>
<td>1.17</td>
</tr>
<tr>
<td>DiCNN1</td>
<td>0.9492</td>
<td>6.2771</td>
<td>3.6487</td>
<td>0.9261</td>
<td>1.13</td>
</tr>
<tr>
<td>DiCNN2</td>
<td>0.9448</td>
<td>7.2012</td>
<td>3.7063</td>
<td>0.9299</td>
<td>0.98</td>
</tr>
</tbody>
</table>

The best and second-best results are marked in bold and italic.

Fig. 4 displays the images of reduced-resolution experimental results. It shows that the pansharpened images yielded by CNN-based methods look much more similar to the ground-truth, without noticeable artifacts or spectral distortions. Fig. 5 shows the detail images, which are produced with the difference between the pansharpened HRMS image and the pre-interpolated LRMS image. The ground-truth details are achieved by the subtraction between the full-resolution MS image and the pre-interpolated one. The detail images are also in favor of the aforementioned observations, as it can be seen in the central circle area. For the CNN-based methods, the performances are hard to distinguish, but by investigating the spectral preservation of ground objects with small sizes, it is clear that DiCNN1 helps to impede spectral distortion more efficiently, as it can be seen in the bottom leftmost part of Fig. 4(h)–(k). Fig. 6 shows the residual images that are generated by the difference between the pansharpened HRMS image and the ground-truth image. From Fig. 6, we can see that the proposed methods exhibit very good performance.

Fig. 7 displays the full-resolution experimental results. The CNN-based methods exhibit sharper results than the other tested methods, especially in the vegetation areas. DiCNN1, PNN,
Fig. 4. Pansharpening results for a Worldview-2 dataset (composited with red, green, blue bands). (a) Ground-truth. (b) EXP. (c) GSA. (d) PRACS. (e) ATWT. (f) BDSD. (g) GLP-CBD. (h) PNN. (i) DRPNN. (j) DiCNN1. (k) DiCNN2.

Fig. 5. Detail images of the Worldview-2 dataset. (a) Ground-truth. (b) GSA. (c) PRACS. (d) ATWT. (e) BDSD. (f) GLP-CBD. (g) PNN. (h) DRPNN. (i) DiCNN1. (j) DiCNN2.

Fig. 6. Differences between the pansharpened images and the ground-truth of the Worldview-2 dataset. (a) EXP. (b) GSA. (c) PRACS. (d) ATWT. (e) BDSD. (f) GLP-CBD. (g) PNN. (h) DRPNN. (i) DiCNN1. (j) DiCNN2.
Fig. 7. Full-resolution pansharpening results for the WorldView-2 dataset. (a) PAN image. (b) EXP. (c) GSA. (d) PRACS. (e) ATWT. (f) BDSD. (g) GLP-CBD. (h) PNN. (i) DRPNN. (j) DiCNN1. (k) DiCNN2.

TABLE III
QUALITY INDEXES OF DIFFERENT PANSHARPENING METHODS UNDER REDUCED-RESOLUTION QUALITY ASSESSMENT ON A 256 × 256 SUBSCENE OF THE IKONOS DATASET

<table>
<thead>
<tr>
<th>Reference</th>
<th>Q4</th>
<th>SAM</th>
<th>ERGAS</th>
<th>SCC</th>
<th>Time(s)</th>
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</thead>
<tbody>
<tr>
<td>EXP</td>
<td>0.5791</td>
<td>5.4338</td>
<td>5.7489</td>
<td>0.5453</td>
<td></td>
</tr>
<tr>
<td>GSA</td>
<td>0.8083</td>
<td>5.1063</td>
<td>4.1467</td>
<td>0.7583</td>
<td>0.73</td>
</tr>
<tr>
<td>PRACS</td>
<td>0.7843</td>
<td>5.1175</td>
<td>4.2096</td>
<td>0.7646</td>
<td>0.61</td>
</tr>
<tr>
<td>ATWT</td>
<td>0.8036</td>
<td>5.1198</td>
<td>4.0957</td>
<td>0.7622</td>
<td>0.49</td>
</tr>
<tr>
<td>BDSD</td>
<td>0.8141</td>
<td>5.4020</td>
<td>4.2070</td>
<td>0.7583</td>
<td>1.15</td>
</tr>
<tr>
<td>GLP-CBD</td>
<td>0.8121</td>
<td>5.0884</td>
<td>4.0857</td>
<td>0.7591</td>
<td>0.52</td>
</tr>
<tr>
<td>PNN</td>
<td>0.8846</td>
<td>4.8722</td>
<td>3.1783</td>
<td>0.8836</td>
<td>2.44</td>
</tr>
<tr>
<td>DRPNN</td>
<td>0.8995</td>
<td>4.5546</td>
<td>2.9513</td>
<td>0.9018</td>
<td>1.19</td>
</tr>
<tr>
<td>DiCNN1</td>
<td>0.9120</td>
<td>4.3359</td>
<td>2.8532</td>
<td>0.9091</td>
<td>1.38</td>
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<tr>
<td>DiCNN2</td>
<td>0.9003</td>
<td>4.4757</td>
<td>2.9104</td>
<td>0.9027</td>
<td>1.06</td>
</tr>
</tbody>
</table>

The best and second-best results are marked in bold and italic. and DiCNN2 slightly overpass DRPNN in terms of reducing artifacts.

B. Experiment 2: IKONOS Hobart Dataset

The dataset represents an urban and harbor area of Hobart, Australia. It was acquired by the IKONOS sensor, which collects data in the visible and near-infrared spectrum ranges. The MS sensor is characterized by four bands (blue, green, red, and near infrared) and also a PAN channel with band range from 450 to 900 nm. The resolution of MS is 4 m and PAN is 1 m. The radiometric resolution is 11b. Different areas with size of 256 × 256 pixels are used for reduced-resolution and full-resolution experiments, respectively.

Table III tabulates the results of our reduced-resolution quality assessment on the IKONOS Hobart dataset. Similar phenomena to the ones observed with the previous WorldView-2 dataset can be appreciated. Specifically, CNN-based methods achieve better pansharpening quality than the CS-based and MRA-based methods. DiCNN1 achieves the highest Q4, SAM, ERGAS, and SCC scores, while PNN is the most time consuming. DiCNN2 achieves the least computational time among CNN-based methods.

Fig. 8 displays the reduced-resolution experimental results. As it can be observed, CS/MRA-based methods exhibit poorer pansharpening results than CNN-based methods, as it can be seen in the edges of roofs shown in Fig. 8(c)–(g). Furthermore, DiCNN1 and DiCNN2 look most similar to the ground-truth in terms of spectral fidelity, as it can be seen in the vegetation area in the top left part of Fig. 8(j) and (k). Fig. 9 shows the detail images learned from various methods. They also support the previous observations and, additionally, confirm that DiCNN1 performs slightly better than DiCNN2 in terms of edge restoration, as it can be seen in the circle vegetation area in the bottom leftmost part of Fig. 9(i) and (j). Fig. 10 displays the full-resolution experimental results on IKONOS Hobart dataset. Similar observations can be made with regards to the experimental results reported for the WorldView-2 Washington dataset.

C. Experiment 3: Quickbird Sundarbans Dataset

The dataset represents a forest area of Sundarbans in India. It was obtained by the QuickBird sensor, which provides a high-resolution PAN image with spectral cover range from 760 to 850 nm and with resolution of 0.6 m, and a four-band (blue, green, red and near infrared) MS image with resolution of 2.4 m. The radiometric resolution is also 11b. We selected different areas with size of 256 × 256 pixels for our reduced-resolution and full-resolution experiments, respectively.

Table IV shows the reduced-resolution quality assessment on the Chilika Lake dataset. We can easily conclude that similar phenomena also arise in this dataset. CNN-based methods achieve better pansharpening quality than CS-based and MRA-based methods. DiCNN1 overpasses others in terms of Q4, SAM, ERGAS, and SCC scores. DiCNN2 is the fastest among CNN-based methods, with comparable performance to DRPNN.

Fig. 11 displays the reduced-resolution experimental results. DiCNN1, DiCNN2, and DRPNN look much more similar to the original MS image, but DiCNN2 exhibits less ringing artifacts, such as the edges of the lakes in the leftmost part of Fig. 11(i)–(k). This phenomenon occurs more frequently in PNN. Meanwhile, EXP and PRACS result in significant


Fig. 8. Pansharpening results for IKONOS dataset. (a) Ground-truth. (b) EXP. (c) GSA. (d) PRACS. (e) ATWT. (f) BDSD. (g) GLP-CBD. (h) PNN. (i) DRPNN. (j) DiCNN1. (k) DiCNN2.

Fig. 9. Detail images of IKONOS dataset. (a) Ground-truth. (b) GSA. (c) PRACS. (d) ATWT. (e) BDSD. (f) GLP-CBD. (g) PNN. (h) DRPNN. (i) DiCNN1. (j) DiCNN2.

Fig. 10. Full-resolution pansharpening results for the IKONOS dataset. (a) PAN image. (b) EXP. (c) GSA. (d) PRACS. (e) ATWT. (f) BDSD. (g) GLP-CBD. (h) PNN. (i) DRPNN. (j) DiCNN1. (k) DiCNN2.
Fig. 11. Pansharpening results for the Quickbird dataset. (a) Ground-truth. (b) EXP. (c) GSA. (d) PRACS. (e) ATWT. (f) BDSD. (g) GLP-CBD. (h) PNN. (i) DRPNN. (j) DiCNN1. (k) DiCNN2.

Fig. 12. Detail images of the Quickbird dataset. (a) Ground-truth. (b) GSA. (c) PRACS. (d) ATWT. (e) BDSD. (f) GLP-CBD. (g) PNN. (h) DRPNN. (i) DiCNN1. (j) DiCNN2.

Fig. 13. Full-resolution pansharpening results for the Quickbird dataset. (a) PAN image. (b) EXP. (c) GSA. (d) PRACS. (e) ATWT. (f) BDSD. (g) GLP-CBD. (h) PNN. (i) DRPNN. (j) DiCNN1. (k) DiCNN2.

blurring effects. Fig. 12 shows the detail images learned from various methods, which also support the observations mentioned above. Fig. 13 displays the full-resolution experimental results. EXP has apparent blurring effects, whereas PRACS and DiCNN2 lead to subtle blurring effects. Blurring yielded from DiCNN2 is due to the fact that there is only the PAN image as the input of the convolution layers pathway, which makes it possible that the details complement to the LRMS image are learned insufficiently. In the meantime, DiCNN1 exhibits less artifacts than DRPNN and PNN.
It is worth noting that the spectral range of the PAN image in the Quickbird Sundarbans dataset spans only 90 nm wide, which is far narrower than that of the PAN images in WorldView-2 Washington dataset and IKONOS Hobart dataset, i.e., 350 and 402 nm. This implies that, when we perform pansharpening on the Quickbird Sundarbans Dataset, the PAN image will offer far less information to compensate for the spectral range difference between the PAN image and the MS image and mine the useful details. As we have mentioned previously, DiCNN1 and DiCNN2 have different structures. In DiCNN1, both the PAN image and the LRMS image are forwarded to the convolutional pathway, whereas in DiCNN2 only the PAN image is fed into the convolutional pathway, which means that DiCNN1 comprises two sources of information in its convolutional pathway and, hence, it exhibits higher potential to acquire information that is complementary to the low-resolution MS image. In contrast, DiCNN2 heavily relies on the PAN image to learn useful details for pansharpening. As discussed above, compared to DiCNN1, DiCNN2 depends much more on the PAN image to mine details for pansharpening. On the other hand, the PAN image in Quickbird Sundarbans Dataset has far narrower spectral range and, thus, it tends to offer far less information that is useful for pansharpening. Therefore, when both DiCNN1 and DiCNN2 are applied to Quickbird Sundarbans Dataset, DiCNN2 tends to yield worse pansharpening results than those achieved by DiCNN1, as shown in Fig. 11(j) and (k), and Fig. 13(j) and (k).

D. Experiment 4: Transfer Learning

To demonstrate the robustness of DiCNN2 under the situation that the number of bands of the test MS image has varied, we use the WorldView-2 Washington dataset and IKONOS Hobart Dataset in this experiment. Here, DiCNN2 is first trained on the original dataset. Then some of the MS bands are removed, and the final convolutional layers are fine-tuned to accommodate the current number of bands with $1.0 \times 10^4$ training iterations, much less than that in the previous training step. For the WorldView-2 Washington dataset with eight MS bands, four bands are removed. For the IKONOS Hobart Dataset with four MS bands, one band is removed.

Table V shows a quantitative assessment result on the WorldView-2 Washington dataset. As shown in the table, DiCNN2 yields the best scores in all evaluation metrics. It is remarkable that the time DiCNN2 needs for the training phase is less than half of the longest one, which results from the fact that DiCNN2 only needs to fine-tune the final convolutional layer.

We also apply a similar experiment using the IKONOS data. Since the IKONOS dataset consists of four bands, we randomly choose three of them for testing. The four-band dataset is used to train DiCNN2, while the three-band one is applied to fine-tune the last layer of DiCNN2 and train other CNN-based methods.

Table VI tabulates the pansharpening results obtained by different CNN-based methods. As it can be observed, DiCNN2 outperforms others in most quality indexes. In addition, although DiCNN1 attains comparative results with regards to DiCNN2, the training time of the latter is far less than the former.

VI. CONCLUSION AND FUTURE LINES

In this paper, we have developed two CNN-based pansharpening methods, i.e., DiCNN1 and DiCNN2, based on a detail injection framework (DiPAN), which classical CS/MRA-base pansharpening methods can be ascribed into. In our newly developed DiCNN1 and DiCNN2, the MS details are learned in an end-to-end manner, which has explicit physical meaning and avoids separately dealing with injection gains and PAN details, as it is the case in traditional CS and MRA methods. Our DiCNN1 and DiCNN2 methods can gain low initial loss, which tends to yield faster convergence and exhibit excellent pansharpening performance. Particularly, DiCNN2 can additionally realize transfer learning when the type of the MS image or the PAN image changes, which is a highly desirable property.

In the future, we will explore the possibility of designing PNNs with more hidden layers and more complex inter-connections among multiple convolutional layers.
In this appendix, we provide a careful analysis of the efficiency of the proposed approach. The appendix includes two parts. First, we show that the proposed framework has good initialization. Then, we show that the proposed framework has good optimization.

### A. Analysis of the Initialization of the Framework

CNN models are usually formulated as non-convex optimization problems with many local minima [51]–[53]. To solve such optimizations, the iterative gradient descent method is widely used, where the initialization and the gradient are usually critical for the solution.

Intuitively, better initializations are beneficial to attain better gradient descent solutions. Let us investigate such an initialization issue in more detail. For the four PNNs illustrated in Fig. 3, the output of the stacked convolutional layers pathway can be formulated as follows:

\[
Z_3 = W_3 \ast \varphi(W_2 \ast \varphi(W_1 \ast X + B_1) + B_2) + B_3
\]

(13)

where * denotes convolution, \( \varphi(\cdot) \) represents the ReLU activation function, and \( Z_l = W_l \ast \varphi(W_{l-1} \ast \varphi(Z_{l-1}) \) denotes the output of the \( l \)-th convolutional layer. \( Z_l \) is in 3-D data arrangement and thus a three-way tensor, the concept that has been previously mentioned in the description of (8). Note that \( Z_3 \) has specific meanings for different PNNs, where it represents the MS details \( D \) for our DiCNN1 and DiCNN2, the residuals \( R \) for DRRPN, and the pansharpened HRMS image \( M \) for PNN.

In this paper, the initialization of CNN parameters \( W_l \) and \( B_l \) are assumed to follow an i.i.d. zero-mean random distribution and be independent of the neuron output of the \( l-1 \)-th layer \( A_{l-1} = \varphi(W_{l-1} \ast A_{l-2} + B_{l-1}) \). Obviously, the CNN input \( X \) can be used as \( A_0 \). For later use, we present a property about \( Z_3 \) and its proof below as

\[
E\{Z_3^{(1)} Y\} = E\{E\{W_3 \ast \varphi(Z_2)\}^{(1)} + \{B_3\}^{(1)} Y\}
\]

\[
= E\left\{ \sum_{m} \sum_{n} \sum_{l} W_3(m,n,l) \times \varphi(Z_2(m-x,n-y,l-b)) \right\}^{(1)} + E\{B_3^{(1)}\} E(Y)
\]

\[
= E\left\{ \sum_{m} \sum_{n} \sum_{l} W_3(m,n,l) \times \varphi(Z_2(m-x,n-y,l-b)) \right\}^{(1)} Y + 0 \cdot E(Y)
\]

\[
= E \left\{ \sum_{m} \sum_{n} \sum_{l} W_3(m,n,l) \times \left\{ \varphi(Z_2(m-x,n-y,l-b)) \right\}^{(1)} \right\} Y
\]

\[
= 0 \cdot E(Y)
\]

where \( Y \) is a matrix not necessarily independent of \( Z_3 \) and \( \{\cdot\}^{(1)} \) means the unfolding of a three-way tensor along its first mode, and the following:

\[
\{W_3 \ast \varphi(Z_2)\}^{(1)} = \left\{ \sum_{m} \sum_{n} \sum_{l} W_3(m,n,l) \varphi(Z_2(m-x,n-y,l-b)) \right\}^{(1)}
\]

(1)

\[
\times \sum_{m} \sum_{n} \sum_{l} W_3(m,n,l)
\]

\[
\times \left\{ \varphi(Z_2(m-x,n-y,l-b)) \right\}^{(1)}
\]

(15)

are utilized.

We will first justify that our DiCNNs can achieve better initialization. First, consider DiCNN1. Its loss function \( E(\|D + \tilde{M} - Y\|_F^2) \) can be rewritten as

\[
E(\|D + \tilde{M} - Y\|_F^2)
\]

\[
= E\{\text{Trace}(D + \tilde{M} - Y)(D + \tilde{M} - Y)^T\}
\]

\[
= E\{\text{Trace}(D\tilde{D}^T) + \text{Trace}(\tilde{M}\tilde{M}^T) - \text{Trace}(\tilde{M}Y^T) + \text{Trace}(Y\tilde{M}^T) - \text{Trace}(YY^T)\}
\]

\[
= E\{\text{Trace}(D\tilde{D}^T) + 2\text{Trace}(\tilde{M}\tilde{M}^T) - 2\text{Trace}(\tilde{M}Y^T) + \text{Trace}(YY^T)\}
\]

where the equations

\[
\text{Trace}(E(\tilde{M}\tilde{M}^T)) = 0
\]

\[
\text{Trace}(E(\tilde{M}Y^T)) = 0
\]

are utilized, which can be obtained through (14).
Let us now consider PNN; its loss function $E(\|\tilde{M} - Y\|_F^2)$ can be transformed as

$$E(\|\tilde{M} - Y\|_F^2) = E\{\text{Trace}( (\tilde{M} - Y)(\tilde{M} - Y)^T) \}$$

$$= E\{\text{Trace}( \tilde{M}\tilde{M}^T + \tilde{M}Y^T - \tilde{M}^T Y + YY^T ) \}$$

$$= E\{\text{Trace}( \tilde{M}\tilde{M}^T ) - 2\text{Trace}( \tilde{M}Y^T ) + \text{Trace}( YY^T ) \}$$

$$= \text{Trace}(E(\tilde{M}\tilde{M}^T) ) - 2\text{Trace}(E(\tilde{M}Y^T) )$$

$$+ \text{Trace}(E(YY^T))$$

$$= \text{Trace}(E(\tilde{M}\tilde{M}^T)) + \text{Trace}(E(YY^T)) \quad (19)$$

where the equation

$$\text{Trace}(E(\tilde{M}Y^T)) = 0 \quad (20)$$

is involved, which can also be obtained via (14).

Recall that $\tilde{M}$ represents the pre-interpolated LRMS and $Y$ denotes the ideal HRMS. Therefore, $(\tilde{M} - Y)$ represent MS details whose energy tends to be significantly less than that of pre-interpolated LRMS. To compare the initialization of loss function of DiCNN1 shown in (16) with that of PNN shown in (19), we have

$$E(\|\tilde{D} + \tilde{M} - Y\|_F^2) = E(\|\tilde{M} - Y\|_F^2)$$

$$= \text{Trace}(E(\tilde{D}\tilde{D}^T) ) + \text{Trace}(E(\tilde{M}\tilde{M}^T) )$$

$$- 2\text{Trace}(E(\tilde{M}Y^T) ) + \text{Trace}(E(YY^T) )$$

$$= \text{Trace}(E(\tilde{D}\tilde{D}^T) ) + \text{Trace}(E(\tilde{M}\tilde{M}^T) $$

$$- 2\text{Trace}(E(\tilde{M}Y^T) ) - \text{Trace}(E(YY^T) )$$

$$= \text{Trace}(E(\tilde{M}\tilde{M}^T)$$

$$- 2\text{Trace}(E(\tilde{M}Y^T) ) - \text{Trace}(E(\tilde{M}\tilde{M}^T)$$

$$= \text{Trace}(E(\tilde{M}\tilde{M}^T)$$

$$- 2\text{Trace}(E(\tilde{M}Y^T) ) - 2\text{Trace}(E(\tilde{M}(Y^T + \tilde{M}^T - \tilde{M}^T) )$$

$$= \text{Trace}(E(\tilde{M}\tilde{M}^T)$$

$$- 2\text{Trace}(E(\tilde{M}Y^T) ) - 2\text{Trace}(E(\tilde{M}(Y^T - \tilde{M}^T) )$$

$$= 2\text{Trace}(E(\tilde{M}(\tilde{M}^T - Y^T) ) - \text{Trace}(E(\tilde{M}\tilde{M}^T))$$

$$< 0 \quad (21)$$

where the equation

$$\text{Trace}(E(\tilde{D}\tilde{D}^T) ) = \text{Trace}(E(\tilde{M}\tilde{M}^T)) \quad (22)$$

is utilized during the derivation from step 2 to step 3. This is reasonable, as $\tilde{D}$ and $\tilde{M}$ stand for the outputs of convolutional layers pathways of DiCNN1 and PNN, respectively. In the initial phases of these two CNNs, their convolutional layers pathways have similar structure, similar inputs, and the same distributed network parameters. Moreover, the diagonal entries of $MM^T$ are always greater than or equal to zero. But, in a real image scenario, it is impossible that all of the diagonal entries are equal to zero. Accordingly, we have

$$\text{Trace}(E(\tilde{M}\tilde{M}^T)) > 0. \quad (23)$$

Taking a close inspection of the term $2\text{Trace}(E(\tilde{M}(\tilde{M}^T - Y^T) ))$ in the last equality of (21), we find that $(\tilde{M}^T - Y^T)$ exactly represents the ideal MS details whose energy should account for small portion that of the HRMS image and, thus, we have

$$\text{Trace}(E(\tilde{M}\tilde{M}^T)) > 2|\text{Trace}(E(\tilde{M}(\tilde{M}^T - Y^T) ))|. \quad (24)$$

After using (23) and (24), problem (21) results in

$$E(\|\tilde{D} + \tilde{M} - Y\|_F^2) < E(\|\tilde{M} - Y\|_F^2). \quad (25)$$

In summary, we can conduct that, the initial loss of DiCNN1 is smaller than that of PNN. For verification, let

$$T_1 = \text{Trace}(E(\tilde{M}\tilde{M}^T))$$

and

$$T_2 = 2|\text{Trace}(E(\tilde{M}(\tilde{M}^T - Y^T) ))|$$

be the two traces in (24); Table VII illustrates $T_1$ and $T_2$ computed on three real datasets, which clearly shows that $T_1 \gg T_2$, verifying that DiCNN1 has a better initialization than PNN.

### B. Analysis of the Optimization of the Framework

Since the representations for the gradients are sophisticated and incomparable, it is difficult to quantitatively assess the influence of the gradients on the optimization processes of the four PNNs. Here, we resort to an empirical analysis instead. Fig. 14 illustrates the training losses of the four CNN methods on three datasets. It is observable that the initial losses of DiCNN1 and DiCNN2 are less than those of PNN and DRPNN, corresponding to the theoretical analysis presented earlier in the Appendix A, which means that DiCNN1 and DiCNN2 can achieve better initializations. PNN not only exhibits worse initialization, but also its iteration process (including its gradient) does not change the inferior tendency of its loss. During the iterative process, PNN always yields a loss higher than that of DiCNN1 and DiCNN2. That is, the impact of the gradient-based iteration process is not strong enough to compensate for the loss resulting from an inappropriate initialization. DRPNN exhibits the worst initialization. Although its gradient-involved iterative process makes its loss drop fast, it is still always higher than that of DiCNN1 during the iterative process.

### Table VII

<table>
<thead>
<tr>
<th>Dataset</th>
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<td>Quickbird</td>
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<tr>
<td>Worldview-2</td>
<td>607.1628</td>
<td>20.2275</td>
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This article has been accepted for inclusion in a future issue of this journal. Content is final as presented, with the exception of pagination.
Fig. 14. Training losses of DiCNN1, DiCNN2, PNN, and DRPNN. (a) IKONOS image. (b) Quickbird image. (c) WorldView-2 image.

REFERENCES


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